## EINCRYPTION KEY MANAGEMENT

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By

MAjOR B P SINGH
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## CERTIFICATE

This is to certify that the dissertation entitled 'Encryption Key Management submitted in partial fulfillment of requirements for the degree of Master of Technology in Electrical Engineering of Military College of Electronics and Mechanical Engineering, Secunderabad is a record of work carried out by Major Bhanu Pratap Singh under my guidance.

The matter presented in this paper has not been submitted for the award of any other degree, diploma or certificate.

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Maj Bhanu Partap Singh has presented the dissertation on Encryption Key Management at MCEME on 24 July 98 and has fulfill the requirement to the best of my satisfaction


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## INTRODUCTION

The need to keep certain messages secret has been appreciated for thousands of years People were active to realize the advantages to be gained from intercepting secret information: and this has led to a continuos, fascinating battle between the 'codemakers' and the 'codcbreakers'. The broad spectrum for this contest is the commonication medium which has changed considerably over the years. The society is now highly dependent on modern, fast and accurate means of transmitting messages. Along with the old method of communication systems such as post, courier service, now a day radios, television telephone, telex and high speed data links are ... ailable In each mode of transmission the aim remains to have a cheaner and reliable system. There are, however, a number of situations where the information is confidential, and where the interceptor will gain immensely from the knowledge gained by monitoring the information circuit. In such situation, the commonicants must conceal the content of the their message. At some occasion it may be good enough to concert the information from a casual listener from understanding the message, but there are other times when it is crucial that even the most determined interceptor must not be able to deduce it

The need of concealing the information before it is transmitted has increased over a period of time. The common-man has become aware that information pertaining him is transmitted over various data links and he feeis that if not all some information is confidential and hence Inauthorised personnel should not have access to it, more so, shall not be able th alter it. In such situations the communicants have no alternative but to give attention to secu ity of their transmission.

The cryptographer's use various methods to encipher the information before the same is communicated. There are various hardware and software available for this purpose. In present day scenario where mode of communication are available they need to be reliable in terms of stability and accuracy such that no portion of the enciphered information is allered even by mistake as the receptor will not be able to decipher the message. Not only the information being transmitted should reach the adversary but he should also not be able to break the key and the key pattern being used to decipher the content of the message transmitted or being transmitted.

To achieve this aim the cryptographer has to pay attention on the Key Management aspect as well. While addressing to the problem of key management a number of question arise like, - how large should be the key, how often should it be changed, by which method it should be changed, how it should be generated and, how it should be transmitted?

## Classical Cryptography

The fundamental objective of cryptography is to enable two people, usually referred to as Alice and Bob, to communicate over an insure channel in such a way that an opponent, Oscar, cannot undersiand what is being said This channel could be a telephone line computer network, for exampie. The information that Alice wants to send to Bob, which we call "plaintext," can be English text, numerical data, or anything at all - its structure is completely arbitrary. Alice encrypts the plaintext, using a predetermined key, and sends the resuling ciphertext over the channel. Oscar, upon seeing the papertext in the channel by eves dropping. cannot determine what the plaintext was; but Bob, who knows the encryption key, can decrypt the ciphertext and reconstruct the plaintext.

This concept is described more formally using the following mathematical notation.

DEFINITON: A cryptosystem is a five-tuple ( $\mathrm{P}, \mathrm{C}, \mathrm{K}, \mathrm{E}, \mathrm{D}$ ), where the following conditions are satisfied:

1. P is finite set of possible plaintexts.
2. C is a finite of possible ciphertexts.
3. K , the keyspace, is a finite set of possible keys.
4. For each $K \in \mathbb{K}$, there is an encrypting rule $e_{k} \in E$ and a corresponding decryption
$d_{k} \in D$. Each $e_{k}: P \rightarrow C$ and $d_{k}: C \rightarrow P$ are function such that $d_{k}\left(\rho_{n}(x)\right)=x$ for every plaintext $x \in P$.

The main property is property 4 . It says that if a plaintext $x$ is encrypted using $\hat{e}_{k}$, and the resulting eiphertext is subsequently decrypted using $d_{h}$, then the original plainext $x$ results

Alice and Bob will employ the following protocol to use a specific cryptosystem. First, they choose a random key $\mathrm{K} \in K$. This is done when they are in the same place and are not being observed by Oscar, or, alternatively, when they do have access to a secure channel, in which case they can be in different places. At a later time, suppose Alice wants to communicate a message to Bob over an insecure channel and message is a string.

$$
X=x_{1} x_{2} \ldots x_{n}
$$

for some integer $n \geq 1$, where each plaintext symbol $x_{i} \in P, 1 \leq I \leq n$. Each $x_{i}$ is encrypted using the encryption key rule $\mathrm{e}_{\mathrm{k}}$ specified by the predetermined key K . Hence, Alice compotes $\mathrm{y}=\mathrm{e}_{\mathrm{k}}\left(\mathrm{x}_{\mathrm{i}}\right), 1 \leq i \leq \mathrm{n}$, and the resulting ciphertext string is $\mathrm{y}=\mathrm{y}_{1} \mathrm{y}_{2} \ldots \ldots \mathrm{y}_{\mathrm{n}}$.


The communication channel
$y=y_{1} y_{2} \ldots \ldots \ldots . y_{n}$ is sent over the chand. When Bob receives $y_{1} y_{2} \ldots y_{n}$, he decrypts it ung the decryption function $d_{k}$, obtaining the original plaintext string, $x_{1} x_{2} \ldots x_{n}$

Clearly, it must be the case that each encryption function $e_{k}$ is an injective function (i.e., one-to-
 For example, if
$y=e_{k}\left(x_{i}\right)=e_{k}\left(x_{2}\right)$
where $x_{1} \neq x_{2}$, then Bob has no way of knowing whether $y$ should decrypt to $x_{1}$ or $x_{2}$. Note that if $\mathrm{P}=\mathrm{C}$, it follows that each encryption function is a permutation. That is, if the set of plantexts and ciphertexts are idcntical, then each encryption function just rearranges (or permutes) the clements of this set.

## modular arithmetic

DEFANTION Suppac a and $b$ are integers, and $m$ is a positive integer. Then we write $a=b$ $(\bmod m)$ if $m$ divides $b-a$. The phrase $\equiv b(\bmod m)$ is read as "a is congruent to $b$ modulo m". The integer $m$ is called the modulo.

Suppose we divide a and b by m, obtaining integer quotients and remainders. where the remainders are between $0 \leq r_{2} \leq m-1$. Then it is not difficult to see that $a=b(\bmod m)$ if and only if $r_{i}=r_{-}$. We will use the notation a mod $m$ (without parentheses) to denote the remander when a is divided by $m$, i.e., the value $i l$ above. Thus $a=b(\bmod m)$ if $a \bmod m=b \bmod m$. If we replace $a b y$ a mod $m$, we say that a is reduced modulo $m$.

Many computer programming languages define a mod $m$ to be the remainder in the range $m+1, \ldots, m-1$ having the same sign as a for example, -18 mod 7 would be -4 , mather than 3 as we defined it above. But for our purposes, it is much more convenient to define a mod malways to be non-negative.

We can now define arithmetic module $m: Z_{m}$ is defined to be the set $(0, . m-1)$, equipped with two operators, $t$ and $x$. Addition and multiplication in $Z_{m}$ work exactly like real addition and multiplication, and the results are reduced modulo $m$

For example, suppose we want to compute $11 \times 13$ in $Z_{16}$. As integers, we have $11 \times 13=143$. To reduce 143 modulo 16 , we just perform ordinary long division; $143=(8 \times 16)+15$, so 143 mod $16=15$, and hence $11 \times 13=15$ in $Z_{16}$.

These defmition of addition and multiplication in 7 , satisfy most of the familiar rules of arithmetic. These properties are listed here

1. addition is closed, i.e, for any $a, b \in 7 \mathrm{~m}, a+b \in Z_{m}$
2. addition is commutative, i.e, for any $a, b \in Z_{m}, a+b=b+a$
3. addition is associative, i.e., for $a, b, c \in 7_{m},(a+b)+c=a+(b+c)$
4. 0 is an addition identify, i.e, for any $a \in Z_{m}, a+0=0+a=a$
5. The additive inverse of any $a \in Z m$ is $m-a$, i.e., $a l(m-a)=(m-a)+a=0$ for any $a \in Z_{m}$
6. multiplication is closed, i.e., for any $a, b \in Z_{i n}, a b \in Z_{m}$
7. multiplication is commutative, i.e., for any $a, b \in Z m a b=b a$
8. multiplication is associative, i.e, for any $a, b, c \in Z_{m},(a, b) c=a(b c)$
9. a multiplicative identity, i.e., for any $\mathrm{a} \in 7 \mathrm{~m}, \mathrm{a} \times 1=1 \times \mathrm{a}=\mathrm{a}$.
10. multiplication distioutes over addition, i.e., for any $a, b, c \in Z \mathrm{~m},(\mathrm{a}+\mathrm{b})+\mathrm{c})=(\mathrm{ac})+(\mathrm{hc})$ and $a(b+c)=a b+a c$.

Properties 1, 3-5 say that $Z_{m}$ forms an algebraic structure called a group with respect to the addition. Since property 4 also holds, the group is said to be abelian.

Properties $1-10$ establish that $Z_{\mathrm{n}}$ is, in fact, a ring. Some familiar examples of rings include the integers $Z$, the real numbers $R$; and the complex numbers $C$. However, these are all infinite rings, and our attention will be confined almost exclusively to finite rings.

 example, to compute $11-18$ in 731 , we can evaluate $11+13 \bmod 31=24$ Altornatively, we can first subtract 18 form 11, oftaining -7 and then compute -7 mod 31-24

## CRYPTO SYSTEMS

## Shift Cibher

let $\mathrm{P}=\mathrm{C}=\mathrm{K}=72 \mathrm{~F}$. For $0 \leq 25$, define
$\mathrm{e}_{k}(\mathrm{x})=\mathrm{x}+\mathrm{K} \bmod 26$ and
$\mathrm{d}_{\mathrm{k}}(\mathrm{y})=\mathrm{y}-\mathrm{K} \bmod 26$
$\left(x, y \in Z_{26}\right)$.

11 is defmed over $7_{26}$ since there are 26 letters in the English alphabet though it could be defmed over Zm for any modulus m . It is easy to see that Shift Cipher forms a cryptosystem as defned above, i.e., $d k\left(e_{k}(x)\right)=x$ for every $x \in Z_{26}$.

REMARK For the particular key $K=3$, the cryptosystem is of en called the Caesar Cipher, witch was purportedly used by Julius Caesar

We would use the Shift Cipher (with a modules of 26) to encrypt ordinary Finglish text by seting up a correspondence between alphabetic and residues modulus 26 as follows: $\mathrm{A} \leftrightarrow 0, \mathrm{~B} \leftrightarrow 1, \ldots, Z$ $\leftrightarrow 25$.

The same is recorded here for future reference:


EXAMPLE:

Suppose the key for a Shift Cipher is $K=11$, and the plaintext is
wewilmeetatmidnight

We first convert the plaintext to a sequence of integers using the specified correspondence, obtaining the following :

| 22 | 4 | 22 | 8 | 11 | 11 | 12 | 4 | 4 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 0 | 19 | 12 | 8 | 3 | 13 | 8 | 6 | 7 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Next, we add 11 to each value, reducing each sum modulo 26 :

$$
\begin{array}{llllllllll}
7 & 15 & 7 & 19 & 22 & 22 & 23 & 15 & 15 & 4 \\
11 & 1 & 23 & 19 & 14 & 24 & 19 & 17 & 18 & 4
\end{array}
$$

Finally, we convert sequence of integers to alphabetic characters, obtaining the ciphertext:

HPHTWWXPPELEXTOYTRES.

To decrypt the ciphertext, Bob will first convert the ciphertext to a sequence of integers, then subtract 11 form each value (reducing modulo 26), and finally convert the sequence of integers to alphabetic characters. In the above example upper case letters are used for ciphertext and lowor case letters for plaintext, in order to improve readability only.

If a cryptosystem is to be of practical use, it should satisfy certain properties. We enumernte two of these properties now.

1. Each encryption function $c_{k}$ and each decryption $d_{k}$ should be efficiently compuabie.
2. An opponent, upon seeing a ciphertext string $\mathbf{y}$, should be unable to determine the key $k$ that was used, or the plaintext string $\mathbf{x}$.

The second property above is defining, in a very vague way, the idea of "security". The process of attempting to compute the key $K$, given a string of ciphertext $y$, is called cryptanalysis. Note that, if Oscar can determine $K$, then he can decrypt y just as Bob woudd, using $d_{k}$. Hence, determining $K$ is at least as determining the plaintext string $x$

## EXAMPLE

Given the ciphertext string :

## JBCRCLQRWCRVNBIENBWRWN,

We successively try the decryption keys $\mathrm{d}_{0}, \mathrm{~d}_{1}$ etc. The following is obtained
 i a bq b $k p q \vee b q u m a i d m a v q \vee m$



 $d$ v w l wfol q w i p h v d y h v q l q h
 $b t u j u d i j o u j n f t b w f t o j o f$ astitchintimesavernine

At this point, we have determined the plaintext and we can stop. The key is $K=9$.

## Substitution Cipher

Substitution ciyptosystem has been used for hundreds of years. In case of substitution cipher we take $P$ and C both to be the 26 -letter English alphabet. We use $Z_{25}$ in the Shif cipher because encryption and decryption are algebraic operation. But in the substitution cinher is is more convenient to operate on alphabetical characters for encryption and decryption.

A key for substitution cipher just consists of a permutation of 26 aphabetic characters The nomber of these permutations is 261 , which is more than $4 \times 10^{20}$. Thus an exhmusive koy search whom computers is infeasible.

## Example

Let $\mathrm{P}=\mathrm{C}=\mathrm{Z}_{25}$. K consists of all possible permutations of the 26
symbols $0,1, \ldots \ldots, 25$. For each permutation $\mathrm{n} \in K$, define
$\mathrm{e}_{\pi}(\mathrm{x})=\pi(\mathrm{n})$
and define
$\mathrm{d}_{\pi}(\mathrm{y})=\pi-1(\mathrm{y})$,
where $\pi-1$ is the inverse permutation to $\pi$.

As the above example indicates, a necessary condition for the cryptosystem to be secure is
 large keyspace may also not guarantee security.

## Vigenere Cipher

In both the Shift cipher and the substitution cipher, once a key is chosen each alphabetic character is mapped to a unique alphabetic character, hence they are called monoalphontin yonen enner system is a polyalphbetic cipher. It uses the encipherment table called the Vigonere snmare In this $\therefore$ : table English alphahets are written in a row and English alphabets are shifted by noe phee in each row, 26 such rows are writen one over the other, with the 'natural' alphabet as an extra colum on the left.

Each letter in the extra column determines a row of the square, while each row represents an additive cipher. Each of these substitution alphabet is then used, in the order of tho segtonon on encipher a single letter. In the most common usage, called the Yigenere einher the mehod of obtaining the sequence involves choosing a keyword (or phrase) If the plan tevt mononge in !onger than the keyword then the sequence is obtaned by remeating it as many times as nocerony then the perind is the length of keyword We can also replace each row of the Vignore ongoro hy ony substation aphabet and then use the new square as discussed above There is one partoniar such square known as beauiort square, in which alphabet are written in the reverse order

## PRACTICAL SECURITY

In order to asses the ractical security of a system one must have an idea of the res.ut. which are likely to be available at the disposal of the expected cryptanalyst. In particular one need to know the computing power available to him. When trying to determine the practical security of a system, one must determine the number of operations or storage elements needed to break it and then decide if it provides enough cover time for the message to be secure. It is also of importance to note that number of operation required does depend on the efficiency of the method of attack. Hence the cryptanalyst always seeks ways of reducing the number of operations. Even when testing one key every microsecond ,to solve a monoalphabetic cipher by trying every key would take about $1.12 \times 10^{13}$ years. In practice, therefore, cryptanalyst must try to find method which do not entail trying every key, but eliminate many possibilities at a time.

## Diffusion and Confusion

The cryptographer use the technique which are called diffusion and confusion. The idea behind diffusion is to 'spread' the statistics of the message space into a statistical structure which involves long combination of the letters in the cryptogram. This is similar to the concept of source coding.

Confusion is to make the relation between the cryptogram and the corresponding key a complex one. This aims to make difficult for statistics to pinpoint the key as having come from any particular area of the key space. In particular, it tries to ensure that the majority of the key is needed to obtain even very short cryptogram, which implies that every message character enciphered will depend on virtually the entire key. Hence forcing the cryptanalyst to find the whole
key simultaneously by making him solve considerably more complex equation then when he was able to find the key piece by piece.

## Shannon's Five Criteria

Shannon made five suggestions in 1940 and since than technology has advanced considerably. His suggested criteria were :
(a) the amount of secrecy offered,
(b) the size of the key,
(c) the simplicity of the enciphering and deciphering operation,
(d) the propagation of error and,
(e) extension of the message.

Criteria (a) need not any discussion as the importance is obvious. The key must be kept secret and ,on occasion, may need to be memorised. Consequently it should be as small as possible Enciphering and deciphering as per Shannon should of course be as simple as possible. If they are done manually, complexity leads to loss of time, errors etc. If done mechanically, complexity leads to a large, expansive machines. With some cipher systems, one error occurring on a transmission can mean that, when the cryptogram is deciphered, whole portion, or even the complete message is garbled. For most communication the error propagation should clearly be minimised. In some cipher system the size of message increases by the enciphering process. For instance use of mulls (i.e adding meaningless characters to swamp the message statistics)causes a larger cryptogram than message. Such a message extension is undesirable for most communication systems.

There appears to be a certain incompatibility between the requirement of each of these files criteria when our message space consist of a natural language. It is probably not possible to satisfy all five but, if one is dropped, it may be possible to satisfy other four. The first criteria cannot be dropped for obvious reasons English.

If we drop (e) and allow unlimited message extension, then we can encipher many extra message and use part of the key to indicate the correct one, still it is not sure that requirement of (b) and (c). will be met. By dropping (d) we can use a block cipher. But again it is not clear that requirements for either (b) or (c) can be achieved, though block cipher may lead to error propagation. Third criteria of Shannon need not be discussed with the present day electronics available to carry out enciphering and deciphering operation. Propagation of error is necessarily not a bad thing at times, the effects of error propagation proves to be advantegeous and at times totally unacceptable as it corrupts the message.

## Worst Case Conditions

In order to assess the security of system following three assumptions are made, which are reforred to as worst case conditions.

C1 The cryptanalyst has a complete knowledge of the cipher system.

C2 The cryptanalyst has obtained a considerable amount of cipher text.

C3 The cryptanalyst knows plaintext equivalent of certain amount of the ciphertext.

In any given situation we will attempt to quantify realistically what we mean by considerable and certain. This will depend on particular system under consideration.

Condition $\mathbf{C l}$ implies that there is no security in the cipher syster. itself and that all security must come from the key. Naturally the cryptanalyst 's task is considerably harder if he does not know the system used and it is now possible to conceal this information to certain extent. It should be clear that $\mathbf{C 2}$ is a necessarily assumption which, in conjuction with $\mathbf{C 1}$ has found the basis of many of our earlier cryptanalitic attacks. It has to be assumed that if a cryptanalyst can intercept communication between two parties, he is likely to be able to intercept others, who may have implied the same key. C3 is the basis of the known plaintext attack which is probably the most important and most commonly used method of breaking cipher. In this case the cryptanaiyst has, possibly by guess work, deduction, or even by planting some one in some way, obtained knowledge of some of the plaintext message prior to its encipherment. The cryptanalyst may, for instance, know that all communication between two sources begin with a particular name and address or a particular phrase or expression

## Stream Cipher Systems

So far discussed cipher systems could be implemented in a reasonably short time, either by hand or by using a mechanical or electro-mechanical machine. The most significant factors in the development of the design of cipher systems were the advent of the computer and then, in the 1960s, the expanding use of microelectronics. They meant that a whole new range 0 . f.nu:.ons were available to the cryptographer. But they also compelled him to increase his mathematical knowledge. Many of these new functions could only be expressed in terms of a mathematical language which was considerably more advanced than any of the mathematical knowledge previously required has been the development of the cipher system greatly influenced by the fact that Shannon had proved the one - time - pad to be unbreakable. Many cryptographers felt that, if they could emulate the one-time-pad system in some way, they would have a system with a guaranteed high security level. They were also encouraged by the fact that, since the 1930 s, many of the mechanical and electro-mechanical machines had operated in a way similar to the one-timepad; in the sense that they produced long sequences of displacements which were applied, character by character, to the plairtext message. However there is one fundamental difference. Unlike the situation for the one-time-pad, a sequence produced by one of these machines is not random; in fact. it is completely determined by the key. Once the key has been set up, the sequence, although certainly as long as the message, is completely predetermined. Nevertheless, by careful choice of the algorithm, it was possible to produce a sequence which appeared to be random, i.e a seguence in which there was no telegraphers that such a system would be highly secure.

The abovo ideas led to the introduction of the stream cipher, illustrated in Figure.


## A Stream Cipher

Thus a stream cipher is a system in which the key is fed to an algorithm which uses the key to generate an infinite sequence. (The algorithm is usually referred to as the sequence generator or keystream generator.) In all practical cases of cipher systems, the algorithm is an example of a finite state machine.

It is important to realize that a stream cipher attempts to utilize confusion, but not di. aici.. This gives it a major advantage over a block cipher; namely that it is not error propagating. For this reason, stream ciphers provide probably the most important method of modern encipherment, since the majority of such systems employ electronic techniques, both the plaintext and the infinite sequence use a character set which has only two possibilities corresponding to on and off. For convenience these are labeled 1 and 0 and the resulting system is called a binary system.

One way of viewing our stream cipher system is a polyalphabetic cipher whose periodicity is governed by the sequence which the algorithm produces. But it is important to realize that, although the sequence has infinite length, this does not mean that the polyalphabetic cipher cannot have finite period. The infinite sequence may have the property that it is merely numerous repetitions of a finite sequence. If this occurs then we say that it is periodic. We call the shortest
repeated sequence a cycle and the length of a cycle is the period of the infmite sequence. If we represent the sequence $\mathrm{S} 1 \mathrm{~S} 2 \mathrm{~S} 3 \ldots$. by $(\mathrm{S} 1)$, then if $(\mathrm{Si})$ has period P we know $\mathrm{Sm}+\mathrm{p}$ for every m . If the period of our output sequence is small, the system will have the same type of drawbacks as the Vignere cipher with short keyboard. It is essential for security that our output sequence should have a large period and that the period should, as an absolute minimum, be at least as long as any message to be cuciphered. For this reason, we will need theorems which tell us when the output sequence has a guaranteed minimum period. A second requirement for our output sequence , again based on our experience in attempting to cryptanalyze Vignette - type ciphers, is that it should appear to be random and, thus, not allow the cryptanalyst to use any known statistical analysis of the language of the system. Thus our two main aims are :

A1 The input key stream sequence must have a guaranteed minimum length for its period. (we will then only enciphers messages which are shorter than this value.)

A2 The ciphertext must appear to be random.

$$
7 H-7231
$$



## DATA ENCREPTION STANDARD

The Data Encryption Standard (DES) specifies an algorithm to be implemented in electronic hardware devices and used for the cryptographic protection of computer data. This publication provides a Complete description of a mathematical algorithm for encrypting and decrypting binary coded information .Encrypting data converts it to an unintelligible form called cipher. Decrypting cipher converts the data back to its original form. The algorithm described in this standard specifies both enciphering and deciphering operations which are based on a binary number called a key. The key consist of 64 binary digits ( 0 ' s or 1's) of which 56 bits are used directly by the algorithm and 8 bits are used for error detection.

Binary coded data may be cryptographically protected using the DES algorithm in conjunction with a key. The key is generated in such a way that each of the 56 bits used directly by the algorithm are random and the 8 error detecting bits are set to make the parity of each 8 -bit byte of the key odd, i.e. there is an odd number of ' 1 ' $s$ in each 8 -bit byte. Each member of a group in common, is used to decipher the data received in cipher form from other members of the group. The encryption algorithm specified in this standard is commonly known among those using the standard. The unique key chosen for use in a particular application makes the results of encrypting data using the algorithm unique. Selectio: of a different key cause the cipher that is produced for any given set of inputs to be different. The cryptographic security of the data depends on the security provided for the key used to encipher and decipher the data.

Data can be recovered from cipher only by using exactly the same key used to encipher it Unauthorized recipients of the cipher who know the algorithm but do not have the conrect key cannot derive the original data algorithmically. However, anyone who does have the key and the algorithm can easily decipher the cipher and obtain the original data. A standard algorithm based on a secure key thus provides a basis for exchanging encrypted computer data by issuing the key used to encipher it to those authorized to have the data.

## DATA ENCRYPTION ALGORITHM

The algorithm is designed to encipher and decipher blocks of data consisting of 64 bits under control of a 64 bit key. Deciphering must be accomplished by using the same key as for enciphering, but with the schedule of addressing the key bits altered so that the deciphering process is the reverse of the enciphering process. A block to be enciphered is subjected to an initial permutation IP, then to a complex key-dependent computation and finally to a permutation which is the inverse of the initial permutation IP-1. The key-dependent computation can be simply defined in terms of function $f$ called the cipher function, and a function KS , called the key schedule. A description of the computation is given in terms of primitive functions which are called the selection function $f$ is givi.a in terms of primitive functions which are called the selection functions $S 1$ and the permutation function P .

## Enciphering

A sketch of the ciphering computation is given in figure.

The 64 bits of the input block to be enciphered are first subjected to the following permutation. called the initial permutation IP:

## IP

$$
\begin{aligned}
& 585042342618102 \\
& 605244362820124 \\
& 625446383022146 \\
& 64564840322416 \\
& 57494133251791 \\
& 595143352710113 \\
& 615345372921135 \\
& 635547393123157
\end{aligned}
$$

That is the permuted input has bit 58 of the input as its first bit, bit 50 as its second bit, and so on with bit 7 as its last bit. The permuted input block is then the input to a complex key-dependent computation described below. The output of that computation, called the pre-output, is then subjected to the following permutation which is the inverse of the initial permutation:
$\mathrm{IP}^{-1}$
$\begin{array}{lllllll}40 & 8 & 48 & 16 & 56 & 24 & 64 \\ 32\end{array}$
$\begin{array}{llllllllllllll}39 & 7 & 47 & 15 & 55 & 23 & 63 & 31\end{array}$
$38646 \quad 1454226230$
$\begin{array}{llllll}375 & 45 & 13 & 53 & 21 & 61\end{array} 29$
$\begin{array}{lllllll}364 & 44 & 12 & 52 & 20 & 60 & 28\end{array}$
$\begin{array}{lllllll}35 & 3 & 43 & 11 & 51 & 19 & 59 \\ 27\end{array}$
$\begin{array}{lllllll}342 & 42 & 1050 & 1858 & 26\end{array}$
33141949175725

That is, the output of the algorithm has bit 40 of the pre-ouput block as its first hit, bit 3 as its second bit , and so on, until bit 25 of the pre-output block is the last bit of the output.
I. et the 64 bits of the impit block to an iteration consist of a 32 -hit biock 1 . followed by a 32 hit block R. Using the notation defined eariier, the input block is than LR

Let $K$ be a block of 48 bits chosen from the 64-bit key. Then the output L'R' of an iteration with input $L R$ is defined by:
(1) $L^{\prime}=R$
$\mathrm{R}^{\prime}=\mathrm{L} \oplus f(\mathrm{R}, \mathrm{K})$, where $\oplus$ denotes bit-by-bit addition modulo 2 .

The input of the first iteration of the calculation is the permuted input block. If $L$ ' $R$ ' is the output of the $16^{\text {th }}$ iteration than $R L^{\prime}$ is the preoutput block. At each iteration a different block K of key bits is chosen from the 64 bit key designated by KEY.

Let KS be a function which takes an integer $n$ in the range from 1 to 16 and a 64 - bit block KEY as input and yiclds an output a 48 -bit block $k_{n}$ which is a permuted selection of bits from KEY. That is
(2) $\quad K_{n}=\mathrm{KS}(n, \mathrm{KEY})$
with $k_{n}$ determined by the bits in 48 distinct bit positions of KEY. KS is called the key schodule because the block $K$ used in the $n^{\prime}$ th iteration of (1) is the block $k_{n}$ determined by (2).

Let the permuted input block be $L R$. Finally , let $L_{0}$ and $R_{0}$ be respectively $L$ and $R$ and $L_{n}$ and $R_{n}$ respectively $L$ ' and $R^{\prime}$ of (1) when $L$ and $R$ are respectively $L_{n-1}$ and $R_{n-1}$ and $K$ is $K_{n}$; that is, when $n$ is in the range from 1 to 16 ,
(3) $L_{n}=R_{n-1}$
$\left.\mathrm{R}_{\mathrm{n}}=\mathrm{L}_{\mathrm{n}-1} \oplus f\left(\mathrm{R}_{\mathrm{n}-1}, \mathrm{~K}_{\mathrm{n}}\right)\right)$

The preoutput block is then $\mathrm{R}_{16} \mathrm{~L}_{16}$.

The key schedule KS of the algorithm is described in detail in the Appendix. The key sciedule produces the $16 \mathrm{~K}_{\mathrm{n}}$ which are required for the algorithm.

## Deciphering

The permutation $I^{-1}$ applied to the preoutput block in the inverse of the initial permutation if applied to the input. Further, from (1) it follows that :
(a) $\mathrm{R}=\mathrm{L}^{\prime}$
$\mathrm{L}=\mathrm{R}^{\prime} \oplus f\left(\mathrm{~L}^{\prime}, \mathrm{K}\right)$

Consequently, to decipher it is only necessary to apply the very same algorithm to an enciphered message block, taking that at each iteration of the computation the same block of key bit K is used during decipherment as was used during the encipherment of the block. This can be expressed as
(5) $\quad R_{n-1}=L_{n}$
$\mathrm{L}_{\mathrm{n}-1}=\mathrm{R}_{\mathrm{n}} \oplus f\left(\mathrm{~L}_{\mathrm{NG}}, \mathrm{K}_{\mathrm{i}}\right)$
where now $\mathrm{R}_{16} \mathrm{~L}_{16}$ is the permuted input block for the deciphering calculation and $\mathrm{L}_{0} \mathrm{R}_{0}$ is a procoutput block. That is, for the decipherment calculation with $R_{16} L_{16}$ as the permuted input, $\mathrm{K}_{16}$ is used in first iteration, $\mathrm{K}_{15}$ in the second and so on, with the $\mathrm{K}_{1}$ used in the $16^{\text {th }}$ iteration.


DES Encipering Computation

## KEY MANAGEMENT

## KEY STRUCTURE

Security of a cipher system depends solely on the choice of the key. This point was highlighted when we saw worst case conditions for the cryptographer. There as we asserted that the cryptographer must be prepared for the cryptanalyst to have full details of the entire system and, in particular, completely understand the algorithm. Given the importance of the key, it is obviously crucial that we pay great attention to the problems of choosing and changing keys. We mus! also consider how the encipherer can tell the receiver the fact that he is changing to a new key

On discussing practicai, realistic systems which means that they are theoretically breakable This must be accepted as a premise. Our problem is to determinc how long it would take to break a particular system and/or to estimate the cost involved. If the time or expense is excessive then, for all practical purposes, we may regard our system as secure. This means we musí attempt to quantify the words excessive in the last sentence. For any given system we must determine the number of operations or storage elements needed to break the key, and then decide if this is large enough for our purposes. This of course is one of the problem with today's sophisticated systems, the solutions is by know means simple. In order to increase the number of operation noeded by cryptanalyst, we must increase the number of possibilities for the key. But this implies incroasing the actual size of the key. Unfortunately, as we increase the size of our key, it may make it more difficult to ensure secure distribution and quick, accurate entry. There are many practical situations where these latter consiraints are very important, and on these occasion, the smallost key is advantageous.

As on we find two conflicting requirements, it is therefore necessary to find the compromise. We should keep our keys as small as possible, while still ensuring that nobody can try every possibility in a reasonable time interval.

## Need For Key Change

Assume that we have selected a key of $x$ bits which initializes the algonithm, i.e. gives the algorithm a starting point, and then use this key to encipher $n$ different messages $m_{1,2} m_{2} \ldots, m_{n}$. If we let $\left|\mathbf{m}_{i}\right|$ denote the number of characters in the message $\boldsymbol{m}_{\mathrm{i}}$ then, for any $j$ satisfying $\left|\leq j \leq\left|\boldsymbol{m}_{i}\right|\right.$, we will let $a_{i j}$ represent the $j^{\text {fin }}$ ciphertext character of $m_{i}$. In order to encipher $m_{1}$ we fire ente" the key. The algorithm, using the key as an initializing process, then produces a pseudo-random sequence which determines the sequence of transformations. Similarly for each subsequent message, we enter the same key and, as a consequence, obtain the same pseudo-random sequence and the same sequence of transformations.

If an interceptor obtains $n$ enciphered messages he will be able to arrange them in the kind of array and from any given columns he knows the same section of the enciphering sequence has been used. Thus he can restrict his attention to the columns in turn. But if we let $\mathrm{m}_{\mathrm{ik}}$ be the $k^{\mathrm{d}}$ plaintext letter of $\boldsymbol{m}_{i}$, then $m_{i k}={ }_{m j k}$ if and only if $a_{i k}=a_{j k}$, and this means that the system used for any given column is merely a monoalphabetic substitution. Furthermore it is essentially additive which, of course, guarantees that knowing the ciphertext equivalent of one character determines the entirs substitution.

The amount of use which the cryptanlyst can make of this observation depends on the size of $n$. If n is large then cleary he can milize it, but for small $n$ it is not at presen cher how much in helps him. Certainly if $n=1$ then the cryptanalyst has learnt nothing. If $n$ is greater than 1 , however, he has further information. Since each column comes from a substitution which is essentially addive and each row represents a message, he can attempt to break each column and use the extra fact $\because:$ that each row must be meaningful to settle any ambiguous positions. The precise way of doing this depends on $n$. If $n$ is large he can use the statistics relating to the frequency of occurrence of each letter to determine the most likely substitutions for each column. The fact that each must be meaningful should soon enable him to make firm decisions about any columns where the frequencics leave any room for chance. But if $n$ is small then there will not be sufficient characters in each columns for the frequency statistics to be reliable. In this case he might find it advantageous to concentrate on the rows and use them to try to determine the substitution alphabets.

The value of information depends on the size of $n$. But for large values on $n$ it can reduce the number of trials considerably.

## Key Distribution

Key distribution is defined as a mechanism by which one party chooses a secret key and transmits it to other party(s).
we have a insecure netwoik of $n$ users. In some of the schemes there is a trusted authority (TA) that is responsible for key distribution and key agreement by verifying the identity of users at both the ends. since the network is insecure we have to guard against the passive adversary whose action are restricted upto eavesdropping on messages that are transmitted over the channcl. we also have to guard against the active adversary who can do following kind of things :
(a) alter message that he observes being transmitted over the network
(b) save message for the reuse at a latter time
(c) attempl to masquerade as various users in the network.

The aim of the active adversary may be the any of the following:
(a) to fool $U$ and $V$ into accepting an "invalid" key as valid. It may be one of the old key that has expired.
(b) to make U and V believe that they have exchanged a key with other when they have not.

## Key Predistribution

In key predistribution the TA gencrates ( ${ }_{2}$ ) keys, and gives each key to a pair of user in the network of $n$ users. To transmit these keys from TA to user we require a secure channel. Though the number of channel required to transmit the keys has reduced but, if $n$ is large the problem remains same.

Thus it is of importance to reduce the amount of information to be passed and stored, while still allowing the pair of user U and V to be able to (independently) compute a secret key Ku, $\because$.

## Blom's Scheme

Let us suppose the network is of $n$ users and the keys are chosen from a finite field $Z p$ where $p>=$ $n$ is prime. Let $k$ be an integer, $1=<k=<n-2$. The value $k$ is the largest size coaltion against
which the system will remain secure. In the Bhom's scheme, the TA will transmit $k+1$ elements of 7p to each user over a secure channel. Each pair of user U, V will be able to compute a key Kv, $K u, v$. The security condition is as follows any set of at most $k$ users disiont from $\{U, V\rangle$ must he unable to determine information about $K u, v=$

Blom's key distribution scheme for $k=1$ is as follows:
(a) A prime number $p$ is made public, and for each user $U$, an element $r_{u} \in Z_{p}$ ) is made public. The element $r_{u}$ must be distinct.
(b) The TA chooses three random elements a, b, c $\in Z_{p}$ (not necessarily distinct), and form the polynomial.
$f(\mathrm{x}, \mathrm{y})=\mathrm{a}+\mathrm{b}(\mathrm{x}+\mathrm{y})+\mathrm{cxy} \bmod p$.
(c) For each user $U$, the $T \wedge$ computes the polynomial
$g_{n}(x)=f\left(x,{ }_{n}\right) \bmod p$
and transmits $g_{u}(x)$ to $U$ over a secure channel. Since $g_{u}(x)$ is a linear polynomial in $x$, it can be written as
$\mathrm{g}_{\mathrm{u}}=\mathrm{a}_{\mathrm{u}}+b_{\mathrm{u}} \mathrm{X}$,
where
$a_{u}=a+b r_{u} \bmod p$
and
$b_{u}=b+c r_{u} \bmod p$
(d) If U and V wants to communicate, then they use the common key
$\mathrm{K}_{\mathrm{u}, \mathrm{v}}=K_{v, u}=f\left(\mathrm{r}_{\mathrm{u}}, \mathrm{r}_{\mathrm{v}}\right)=\mathrm{a}+\mathrm{b}\left(\mathrm{r}_{\mathrm{u}}+\mathrm{r}_{\mathrm{v}}\right)+\mathrm{cr}_{\mathrm{u}} \mathrm{r}_{\mathrm{v}} \bmod p$,
where U computes $K_{u, v}$ as
$f\left(r_{u}, r_{v}\right)=g_{u}\left(r_{v}\right)$
and $V$ computes $K_{v, u}$ as
$f\left(r_{v}, r_{u}\right)=g_{v}\left(r_{u}\right)$.

## Diffie-Hellman Key Predistribution

The scheme is described over $Z p$, where $p$ is prime, though it can be implemented in any finite group in which the discrete logarithm problem is intractable. It is assumed that $\alpha$ is a primitive element of $Z p$, and that the values $p$ and $\alpha$ are publicly known to everybody in the netrork

In the scheme $\operatorname{ID}(U)$ will denote certain identification information for each user $U$ in the network e.g., his name , address etc. Also each user $U$ has a secret exponent address etc. Also each user $U$ has a secret exponent $\mathbf{a}_{4}$ (where $0 \leq \mathfrak{a}_{u} \leq p-2$ ), and the corresponding public value $b_{u}=\alpha^{\mathrm{au}} \bmod p$

The TA will have a scheme with a public verification algorithm $v e r_{\mathrm{TA}}$ and a secret signing algorithm $\operatorname{sig}_{\mathrm{r}}$. Finally, we will implicitly assume that all information is hashed, using a public hash function, before it is signed.

Certain information pertaining to a user $U$ will be authenticated by means of a cortificofe which is issued and signed by TA. Fach user will have a certificate

where $b_{u}$ is formed as described as earlier and, TA does not know the value of $a_{u}$. A certificate for the user $U$ will be issued when $U$ joins the network. Certificate can be stored in a public database. or each user can store his or her own certificate. The signature of the TA on a certificate allows any one in the network to verify the information it contains.

W and $V$ can compute the common key $K_{u, y}:$ ( $x$... nv mod $f$ as follows:
(a) A prime $p$ and a primitive element $\alpha \in Z p$ are made public.
(b) $V$ computes
$K_{u, v}=\alpha^{u u n v} \bmod p=b_{u}{ }^{n v} \bmod p$,
using the public value $b_{u}$ from the U's certificate, together with his own secret value $a_{v}$.
(c) U computes
$k_{u, v}=\alpha^{\text {auiv }} \bmod p=b_{v}{ }^{\text {au }} \bmod p$,
using the public $b_{v}$ from V's certificate, together with his own secret value $a_{u}$

Giving a thought about the security of the system in the presence of a passive or active , Ane $\left.{ }^{-}\right\urcorner$ry. The signature of the TA on users' certificates, effectively prevents W from altering any information on some one else's certificate i.c. the system is secure against active attacks. Hence we need worry only about passive attacks.

So the question arises, can a user $W$ compute $K_{u, v}$, if $W \neq U, V$ ? In other words, given $\alpha^{\text {au }}$ mod $p$ and $\alpha^{\text {mu }} \bmod p$ (but not $a_{u}$ and $a_{v}$ ), is it possible to compute $\alpha$ manv mod $p$ ? This problem is called the Diffie - Hellman problem. It is clear that Diffie - Hellman Kcy Predistribution is secure against a passive adversary if and only if the problem is intractable.

## Kerboros

In the key distribution systems, each pair of user computes its one fixed key. If the same key is used for a long time, the fear remains that it may be compromised. Thus it is often preferable to use an on-line key distribution, where a new session key is produced every time a pair of user wants to communicate (this property is called key freshness).

If on-line key distribution is used, there is no need for any user to store keys to communicate with other user (each user share a key with TA however). Session key will be transmitted on request by the TA. It is the responsibility of the TA to ensure the key freshness.

When $U$ wants to establish communication with $V$, he sends a request to TA for a session key, TA will generate a new random session key K . Also, the TA will record the time at which the request is made as a timestamp, $T$, and specifies the , lifetime, $L$, during which K will be valid. That is, session key $K$ is to be regarded valid from time $T$ to time $T+L$. All this information is crypted and transmitted to U and (eventually) to V . The protocol of transmission of session key using Kerboros is as follows:
(a) U asks the TA for a session key to communicate with V .
(b) The TA chooses a random session key $K$, a timetamp $T$, a lifetime $L$.
(c) The TA computes

$$
m_{1}=e_{K u}(K, I D(V), T, L,)
$$

and

$$
\mathrm{m}_{2}=\mathrm{e}_{\mathrm{Kv}}(\mathrm{~K}, \operatorname{ID}(\mathrm{U}), \mathrm{T}, \mathrm{~L})
$$

and sends $m_{1}$ and $m_{2}$ to $U$.
(d) U uses the decryption function $d_{k u}$ to compute $K, T, L$ and $\operatorname{DD}(V)$ from $m_{1}$. We then computes

$$
\mathrm{m}_{3}=\mathrm{e}_{\mathrm{k}}(\mathrm{ID}(\mathrm{U}), \mathrm{T})
$$

and sends $m_{3}$ to $V$ along with the message $m_{2}$ he recieved from TA
(e) V uses the decryption function $\mathrm{d}_{\mathrm{Kv}}$ to compute $\mathrm{K}, \mathrm{T}, \mathrm{L}$ and $\operatorname{ID}(\mathrm{U})$ from $\mathrm{m}_{2}$. He then uses $\mathrm{d}_{\mathrm{k}}$ to compute T and $\operatorname{ID}(\mathrm{U})$ from $\mathrm{m}_{3}$. He checks that two values of T and $\operatorname{ID}(\mathrm{U})$ are the same. If so then V computes

$$
m_{4}=e_{K}(T+1)
$$

and send it to $U$.
(f) $\quad \mathrm{U}$ decrypts $\mathrm{m}_{4}$ using $\mathrm{d}_{\mathrm{K}}$ and verifies that the result is $\mathrm{T}+1$.

The information transmitted in the protocol is illustrated in the following diagram:


Though there is no formal proof that Kerboros is secure against an active adversary, but on a close look at the features of the Kerbors deduction can be drawn.

As mentioned above, the TA generates $\mathrm{K}, \mathrm{T}$, and L in step (b). In step (c), this information along with $\mathrm{ID}(\mathrm{V})$, is cnciphered using the $\mathrm{Key} \mathrm{K}_{\mathrm{u}}$ shared by U and TA to form $\mathrm{m}_{1}$. Also K , T , L and $\mathrm{ID}(\mathrm{U})$ are encrypted using the key $\mathrm{K}_{\mathrm{v}}$ shared by TA and V to form $\mathrm{m}_{2}$. Both these encrypted messages are sent to U .

U can use his key to decrypt $\mathrm{m}_{1}$, and thus obtain $\mathrm{K}, \mathrm{T}$, and L . He can verify that the current time is in the interval of $\Gamma$ to $T+L$ He can also check that the session key $K$ has been issued for his desired communicant $V$ by verifying the information $\operatorname{ID}(\mathrm{V})$ decrypted from $\mathrm{m}_{1}$.

Next, U will relay $\mathrm{m}_{2}$ to V . As well U will use the new session key K to encrypt T and $\mathrm{ID}(\mathrm{U})$ and send the resulting message $m_{3}$ to V .

When $V$ receives $m_{2}$ and $m_{3}$ from $U$, he decrypts $m_{2}$ to obtain $T, K, L$ and ID(U). Then he uses the new session key $K$ to decrypt $m_{3}$ and he verifies that $T$ and $\operatorname{ID}(\mathrm{U})$, as decrypted from $\mathrm{m}_{2}$ and $\mathrm{m}_{3}$, are the same. This ensures $V$ that the session key encrypted within $m_{2}$ is the same key that was used to encrypt $\mathrm{m}_{3}$. Then V uses Key to encrypt $\mathrm{T}+1$, and sends the result back to U as message $\mathrm{m}_{4}$.

The message $m_{1}$ and $m_{2}$ are used to provide secrecy in the transmission of the session key K . On the other hand, $m_{3}$ and $m_{s}$ are used to key confirmation, that is, to enable $U$ and $V$ to convince each other that they posses the same session key K .

The purpose of the timestamp T and lifelime L is to prevent an active adversary from storing old messages for retransmission at a later stage (this is called a replay attack). This method works because keys are not accepted as valid once as they have expired.

One of the drawback of Kerboros is that all the user in the network should have synchronised clocks, since the current is used to determine if a given session key is valid or not. In practice, it is very difficult to provide perfect synchronism, so some amount of variation in time must be allowed.

## Key Exchange

If one does not want to have on-line key server, then he is forced to use key exch: gan a $^{\circ}$.and agreement protocols to exchange secret keys to keep the flow of information between two subscribers without any adversary to have access of the key or the information. The first and the best known key agreement protocol is Diffe-Hellman Key Exchange.

## Deffie-Hellman Key Exchange:

Let us suppose that $p$ is prime, $\alpha$ is a primitive clement of $Z_{p}$, and that the value $p$ and $\alpha$ are publicly known. Alternatively, they should be chosen by $U$ and communicated to V in the first step of the protocol. Diffie-Meliman Key Exchange protocol is as follows:
(a) U chooses $\mathrm{a}_{\mathrm{u}}$ at random, $0 \leq \mathrm{a}_{\mathrm{u}} \leq p-2$.
(b) U computes $\alpha^{\mathrm{au}} \bmod p$ and sends it to V .
(c) $V$ chooses $a_{v}$ at ra.udom, $0 \leq a_{v} \leq p-2$.
(d) $V$ computes $\alpha^{\text {av }} \bmod p$ and send it to $U$.
(c) U computes $\mathrm{K}=\left(\alpha^{3 y}\right)^{\text {at }} \bmod p \quad$ and
$V$ compules $k \cdot\left(v^{* 1}\right)^{* *}$ mod $f^{\prime}$.
(f) At the end $U$ and $V$ both will compute the same $k e y: K=\alpha^{\text {a"I }} \alpha^{\text {a" }}$ mod $p$.

This protocol is very fothilar to Difie-Helman Key predistribution. The difference is that the exponents $a_{u}$ and $a_{v}$ of ${ }^{4}$ user $U$ and $V$ are chosen a new each time the protocol is run, instead of being fixed. Also in this protocol, both $U$ and $V$ are assured of key fresbness, since the session key depends on both random exponents $a_{u}$ and $a_{v}$.

## The Stacion-fo-station Protocol

Diffei-Hellman Key Exchange is supposed to look like this;


Unfortunately, the protocol is vulnerable to an active adversary who uses an intruder-in-the-middle attack. An intruder-in-the-middle attack on the Diffie-Hellman Key Exchange protocol works in the same way. We will intercept messages between $U$ and $V$ and substitute his own messages, as indicated in the following diagram :


At the end of the protocol, U has actually established the secret key $\alpha^{\text {max } v}$ with W , and $V$ has established a secret key $u^{\text {auv }}$ with $W$. When $U$ tries to encrypt a message to send to $V$, $W$ will be able to decrypt it but V will not. ( A similar situation hold if V sends a message to U .)

Hence, it is essential for U and V to make sure that they are exchanging messages with each other and not with W. Before exchanging key, U and V might carry out a separate protocol to establish each other's identity, for example by using one of the identification schemes. But this offers no protection against an intruder - in-the -middle attack if $W$ simply remains inactive until after $U$ and V have proved their identities to each other. Hence, the key agreement protocol should itself authenticate the participants' identities at the same time as the key is being established. Such a protocol will be called authenticated key agreement.

Station-to-station protocol assumes a publicly known prime $p$ and a primitive element $\alpha$, and it makes use of certificates. Each user $U$ will have a signature scheme with verification algorithm ser, and signing algorithm sigu. The TA also has a signature scheme with public verification algorithm $v e r_{\text {ra }}$. Each user too has a certificate

$$
\mathrm{C}(\mathrm{U})=\left(\mathrm{ID}(\mathrm{U}), v e r_{\mathrm{u}}, \operatorname{sig} \operatorname{TA}\left(\operatorname{ID}(\mathrm{U}), v e r_{\mathrm{u}}\right)\right),
$$

where 11$)(1)$ is identification information of $U$.

The Station-to-Station protecol (or STS) is as follows:
(a) U chooses random number $\mathrm{a}_{\mathrm{u}}, 0 \leq \mathrm{a}_{u} \leq p-2$.
(b) U computes

$$
\alpha^{\text {iut }} \bmod p
$$

and sends it to V .
(c) $V$ chooses random number $a_{v}, 0 \leq a_{v} \leq p-2$.
(d) $V$ computes $\quad \alpha^{\text {av }} \bmod p$, then he computes

$$
\mathrm{K}=\left(\alpha^{\mathrm{av}}\right)^{\mathrm{av}} \bmod p
$$

and

$$
y_{v}=\operatorname{sig} g_{v}\left(\alpha^{\mathrm{av}}, \alpha^{\mathrm{au}}\right)
$$

(c) $V$ sends $\left(C(V), x^{a v}, y_{v}\right.$ to $U$.
(f) U computes

$$
\mathrm{K}=\left(\alpha^{\mathrm{av}}\right)^{\mathrm{au}} \bmod p
$$

He verifies $y_{\mathrm{v}}$ using ver ${ }_{\mathrm{v}}$ and he verifies $\mathrm{C}(\mathrm{V})$ using ver $\mathrm{TA}_{\mathrm{TA}}$.
(g) U computes

$$
y_{u}=s \operatorname{sig} g_{u}\left(\alpha^{a u}, \alpha^{a v}\right)
$$

and he sends $\left(\mathrm{C}(\mathrm{U}), y_{u}\right.$ ) to V .
(h) V verifies $y_{n}$ using ver and he verifics $C(U)$ using ver wa.

The information exchanged in the simplified STS protocol (excluding certificates) is illustrated as follows:


Let's see how secure this is against intruder-in-the-middle-attack. As before, $W$ will intercept $\alpha^{\text {au }}$ and replace it with $\alpha^{a \mathrm{u}} \mathrm{W}$ then receives $\alpha^{\mathrm{av}}, \operatorname{sig}_{\mathrm{g}}\left(\alpha^{\mathrm{av}}, \alpha^{\mathrm{ain}}\right)$ from V . He would like to replace $\alpha^{\mathrm{av}}$ with $\alpha^{a^{2} v}$, as before However, this means that he must also replace sigv $\left(\alpha^{a^{v}}, \alpha^{a^{\prime \prime}}\right)$ by $\operatorname{sig},\left(\alpha^{a^{2} v}, \alpha^{\mathrm{au}}\right)$ Unfortunately for $W$, he can not compute $V$ 's signature on ( $\alpha^{a^{i v}}, \alpha^{\text {an }}$ ) since he does not know $V_{i}$ signing algorithm sigg. Similarly $W$ is unable of replacing $\operatorname{sig}_{u}\left(\alpha^{\mathrm{au}}, \alpha^{\mathrm{a} v}\right)$ by $\operatorname{si} g_{u}\left(\alpha^{a^{\text {au }}}, \alpha^{\mathrm{av}}\right)$ because he does not know U's signing algorithm. This is illustrated in the following figure:

W

$$
\alpha^{a v} \text { cior }\left(\alpha^{a v} \alpha^{a} u\right.
$$

It is the use of signature that thwarts the intruder - in-the -middle attack. The above described protocol does not provide key confirmation but, same can be incorporated by modifying the protocol by defining step (d) as

$$
y_{\mathrm{v}}=\mathrm{e}_{\mathrm{k}}\left(\operatorname{sig} g_{\mathrm{v}}\left(\alpha^{\mathrm{av}}, \alpha^{\mathrm{aul}}\right)\right)
$$

and defining

$$
y_{u}=\mathrm{e}_{\mathrm{k}}\left(\operatorname{sig} g_{u}\left(\alpha^{\mathrm{au}}, \alpha^{\mathrm{av}}\right)\right)
$$

in step (f). The resulting protocol is known as the Station - to -station protocol.

## MTE Key Agrecment Protocol

Matsumoto, Takashima, and Imai have constructed several interesting key agreement protocols by modifying Dife-Vtellman Key Pxhange. These protocols are Known as Mre protocols, do not require that U and V compute any signature. They are two pass protocols since there are only two separate transmissions of information performed (one from $U$ to $V$ and other from $V$ To $U$.

The setting for this protocol is same as for Diffie-Hellman Key Predistribution. We assume a publicly known prime $p$ and a primitive element $\alpha$. Each user $U$ has an ID string, ID(U), a secret exponent $\mathrm{a}_{\mathrm{u}}$ ( $0 \leq \mathrm{a}_{\mathrm{u}} \leq p-2$ ), and a corresponding public value

$$
b_{u}=\alpha^{\sin } \bmod p
$$

The TA has a signature scheme with a (public) verification algorithm vern and a secret signing algorithm sig ${ }_{\text {TA }}$.

Each user $U$ have a certificate
$C(U)=\left(I D(U), b_{u} \operatorname{sig} T_{A}\left(\operatorname{ID}(U), b_{u}\right)\right)$,
where $b_{u}$ is formed as described above.

The MTI key agreement is as follows:
(a) U chooses $\mathrm{r}_{\mathrm{u}}$ at random, $0 \leq \mathrm{r}_{\mathrm{u}} \leq p-2$, and computes

$$
\mathrm{s}_{\mathrm{u}}=\alpha^{\mathrm{nI} \mathrm{\prime}} \bmod p
$$

(b) $U$ sends ( $\left.C(U), s_{u}\right)$ to $V$.
(c) $V$ chooses $\mathrm{r}_{\mathrm{v}}$ at random, $0 \leq \mathrm{r}_{\mathrm{v}} \leq p-2$, and computes

$$
s_{v}=\alpha^{\mathrm{rv}} \bmod p
$$

(d) V sends (C (V), sv. to U.
(e) U computes

$$
\mathrm{K}=\mathrm{s}_{\mathrm{v}}{ }^{\mathrm{au}} \mathrm{~b}_{\mathrm{v}}{ }^{\text {u }} \bmod p,
$$

Where he obtains the value $b_{v}$ from $C(V)$ : and $V$ computes

$$
\mathrm{K}=\mathrm{s}_{\mathrm{u}}{ }^{\text {av }} b_{\mathrm{i}}{ }^{\mathrm{rv}} \bmod p,
$$

where he obtains the value of $b_{u}$ from $C(U)$.

At the end both $U$ and $V$ computes the same key

$$
\mathrm{K}=\alpha^{\mathrm{ru} \mathrm{av}+\mathrm{rvau}} \bmod p
$$

looking at the security of the scheme it is pertinent that security of the Mre protocol apainst passive adversary is exactly the same as the Diffic-Hellman problem. The threat of active adversary during an intruder - in- the -middle- attack still appears in absence of any signature protocol. Indeed, it is possible that W might alter the values that U and V send each other. A typical scenario that might arise is as follows:


In this situation, $U$ and $V$ will compute different keys: $U$ will compute

$$
K=\alpha^{r u a v+r v a u} \bmod p,
$$

while V will compute

However, neither of the key computation can be carried out by W, since it require knowledge of secret exponents $a_{u}$ and $a_{v}$, respectively. so even though $U$ and $V$ have computed wince.a keys, which are of no use to them, neither of those keys can be computed by W(assuming the problem of the Discreet Log problem). Hence U and V are assured that the other is the only user in the network that could compute the key that they have computed. This property is also called implicit key authentication.

## Conclusion

The study of cipher system is one of the most rapidly expanding modern sciences. The revolution in microchip technology has resulted in increasing use of electronic means of data communication and a corresponding need for security in the transmission network. The encryption system becomes debited to the development of electronics, because of which the requirement of the cryptology has increased a many fold during last few years across the globe, other than the military requirement.

Another consequence of these recent developments is that the cost of cipher system has been sustainable reduced. This in turn, implies that the encryption devices are open to the man on the street apart from the government official use. As the number of cipher system increase, it is also necessary to develop new techniques.

In cryptography it is not enough to merely to decide over a good algorithm only, or the properties of the transmission medium are adequate, or the way the user want to employ the system is reasonable; the system is not complete unless we consider every aspect of the system or system as a whole. If a single detail changes the designer may need to change the whole system. While designing a cryptology system one has to take a look from not only the encipherer's decrypter's angle but also from the view of the passive and active adversary also to ensure that his system is guarded against any interception at least during the time the information should remain concealed.

## BIELIOGRAPHY

1. APPLIED CRYPTOGRAPHY, BY BRUCE SCHNEIER, 1996 PUBLICATION, ISBN 0-471-59756-2.
2. CRYPTOGRAPHY AND SECURE COMMUNICATION, BY MAN YOUNG RHEE ISRN 0-77-112502-7.
3. CRYPTOGRAPHY AND DATA SECURITY, BY DENNING, JANUARY 1983 PUBLICATION, ISBN 0-201-10150-5
4. CRYPTOGRAPHY THEORY AND PRACTICE, BY DOUGLAS R. STINSON, 1996 PUBLICATION.
5. CIPHER SYSTEMS. THE PROTECTION OF COMMUNICATIONS. BY HENRY BEKER AND FRED PIPER,, 1982 PUBLICATION, ISBN 7198-2611X.
6. COMPUTER NETWORKS, BY ANDREW S. TANENBAUM, SECOND EDITION, MAY 1996, ISBN 81-203-0621-X.
