# SIMULATION OF SATELLITE COMMUNICATION 

## RANDOM MULTIPLE ACCESS PROTOCOL

Dissertation submitted to<br>Jawaharlal Nehru University<br>in partial fulfilment of the<br>requirements for the award of the degree of<br>MASTER OF TECHNOLOGY<br>IN<br>COMPUTER SCIENCE AND TECHNOLOGY<br>by

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## CERTIFICATE

This is to certify that the thesis entitled " SIMULATION OF SATELLITE COMMUNICATION RANDOM MULTIPLE ACCESS PROTOCOL " being submitted by me to Jawaharlal Nehru University, in partial fulfilment of the requirements for the award of the degree of Master of Technology in Computer Science and Technology is a record of original work done by me under the supervision of Prof. Karmeshu and Mr. S. Madan, School of Computer and Systems Sciences during the Monsoon Semester, 1994.

The result reported in this thesis have not been submitted in part or full to any other University or Institution for the award of any degree etc.


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## CHAPTER 1

## INTRODUCTION

The burgeoning technology of satellite communication opens up various horizons in the field of state-of-the-art communictions.The whole globle is brought into unison, just by hopping the data via a satellite. These distances cann't obviously be covered otherwise, by laying down fibre optics cables etc. The wideband data services supported by the satellite communication, encompasses all the needs of technical as well as commercial world.

To make this technology more efficient and cost effectipe there should be a mechanism which extends this facility to large number of users with a better quality.

In view of the growing needs of day to day communications, the multiple access network suits best for this purpose. It allows a large number of users share the same channel. For this many protocols have been developed to fulfill the requirement. A protocol in contrast, is a set of rules governing the format and meaning of the frames, packets, or messages that are exchanged by the pear entities within a layer[4]. These protocols basically scan through a random access on one end to a pre-assigned access on the
other end. The limitation of other networks are given in Chapter 2.

A multiple access scheme proposed by W.W.Wu[2], which has relatively some advantages over other schemes of such as high throughput, simultaneous transmissions toleration and support a large number of users. The scheme called Random Multiple Access is defined as a Time-Frequency (T-F) system utilizing speed spectrum, pulse address and random transmission principles. In this there is no need to check for channel occupancy. In RMA, each user is assigned to a unique sequence of code words, which is an entry to a discrete $T-F$ matrix. So the strategy of code sequence generation is very important. It provides controlled overlapping between any two sequences used in the system. It also provides a large number of coded sequences to accommodate large number of traffic users.

The work which is presented in this project in a systematic way as follows:-
(a) Theoretical background of Random Multiple Access Technique proposed by Wu[2]
(b) Computer Program in PASCAL to generate RMA code sequences using wu algorithm.
(c) Simulation of a network where transmission takes place randomly and study the result obtained in terms of channel throughput with varying offered traffic load.

This algorithm can be implemented to VLSI and desired time, number of transistors, execution time etc., can be found out and finally a layout can be generated.

As it is clear from the algorithm that we require adder, shifter, multiplier, $B$ to $D$ converter and $D$ to $B$ converters, filters, comparators etc.

In Chapter 2 comparison of a RMA scheme with other schemes and RMA code generation algorithm are explained. Chapter 3 gives RMA scheme representation works and system modelling and simulation. Chapter 4 is fully devoted to the results of the simulation. Chapter 5 which is most important chapter contains the conclusions. In Appendix 1 the simulation flow charts and programming code in Pascal are attached.

## CHAPTER 2

## THEORY OF RXMA SCHEME

Using multiple access process, various protocols have been developed. The relative merits and demerits of some ofthose are as follows:

### 2.1 Comparison with Other Schemes

When the number of users becomes very large and number of packets vary unpredictably, pre-assigned access schemes have some limitations i.e.
(i) In Time division multiple access (TDMA), the number of time slots per frame are restricted by the speed of transmission so, we require timing jitter and guard time.
(ii) Because of the bandwith restriction the number of frequency division are limited. If we increase the frequency bandwidth the oscillator stability problem arises.
(iii) In case of basic demand schemes the source identification, channel conditions, message routing, tracking and control bog down the system processes when the number of users become very large.
(iv) Pure ALOHA is suitable for large users and it in a low duty cycle traffic network but has no tolerance for a simultaneous packet transmissions and has maximum throughput of just 18\%[4].
(v) CDMA (Code division multiple access) supports simultaneous users but because of low number of orthogonal sequences it can not entertain large number of users.

A significant improvement in the quality of a transmission channel may be obtained if codes are properly chosen and decoding techniques are efficiently applied RMA differs from CDMA and PAMA, in the RMA does not use pseudonoise or other direct sequences techniques.

### 2.2 RMA Scheme

A RMA code word is defined as a collection of $n$ symbols. The code symbols are the elements of a Timefrequency ( $T-F$ ) matrix $M$. It has same spectrum spreading property as code division multiple access (CDMA), and the addressing principle as pulse addressing multiple access (PAMA). The total number of symbols in $T F$ matrix $M$ is given by $M=n x f$. Where $n$ is the number of time divisions and $f$ is the number of frequency divisions.

The objective is to construct a sequence of m-ary nxf symbol so that a pair of sequences represents binary
signaling from a particular station. If the sequences are completely orthogonal, maximum cross-correlation result in a low probability of error. However, the number of such sequences would then be highly límited as in case of CDMA. Hence, one overlapping symbol in considered in order to increase the number of such sequences. This is expected to result in some graceful degradation due to collisions the high traffic cases which have been studied through simulation is the present work.

Code transmission and detection can be illustrated by an example[5]. Let us divide a given system bandwith and time frame into three divisions i.e. $n=f=3$

$$
M=\left[\begin{array}{lll}
0 & 1 & 2 \\
3 & 4 & 5 \\
6 & 7 & 8 \\
\mathrm{t}_{\mathrm{o}} & \mathrm{t}_{1} & \mathrm{t}_{2}
\end{array}\right] \begin{aligned}
& \mathrm{f}_{2} \\
& \mathrm{f}_{1} \\
& \mathrm{f}_{\mathrm{o}}
\end{aligned}
$$

We further assume that a binary '1' represented by the code word $(3,1,2)$ and binary ' $O$ ' by $(6,4,8)$ then we have

$$
\begin{aligned}
& 1=f_{1} t_{0}+f_{2} t_{1}+f_{2} t_{2} \\
& o=f_{0} t_{0}+f_{1} t_{1}+f_{0} t_{2}
\end{aligned}
$$

A set of frequency synthesizers along with the delay units generate the corresponding codes sequence at the
output of the transmitter depending upon binary input received.


#### Abstract

The receiver detects this code sequence through a set of filters and delay units and companies the transmitted symbols with stored values to check for any error.


### 2.3 Principles of Code Generation

The receiver of the system performs the inverse transformation from a sequence of multiple level symbols back to binary digits. The error performance and system efficiency are mostly affected by the construction of the multiple level symbol sequences for any given number of access stations. In this section, therefore, a systematic procedure is presented. This procedure is optimum in the sense that no other sets of sequences of same length can provides a better sequence distance property.

The code generation algorithm uses the properties of combinatorial sets in deriving the optimum code symbols. Combinatorial theory is a branch of applied mathematics that deals with combination permutation arrangement or enumeration of discrete physical objects to achieve the optimal solution[5]. The key to successful application in to match the structure of the set to the physical parameters of the problem is question or at least as closely as possible. The set can provide an instant optimum guideline, where
other methods fail combinatorial sets consist of two types of sets.
(i) the additive sets and
(ii) the difference sets

Difference sets are considered more useful from a particle point of view [5].
2.4 Procedure of Sequence Construction Algorithm:

The algorithm begins with two matrices $W_{0}$ and $W_{1}$, with size $\left(n^{2}-1\right) x n$ and $(n+1) x n$ respectively. The row of $W_{o}$ consist of the elements of Euclidean geometry difference set and its equivalent sets (algorithm to get difference set is in [5]). The elements in the rows of $W_{1}$ are so construction that the first element in its $0^{\text {th }}$ row can not be any difference module $\left(n^{2}-1\right)$ among the set of residues. A row matrix $R_{j}$ is defined in terms of row of time time-frequency matrix $M$ from $M$ and $R_{j}$ we get $B_{j}$. $A$ set of matrices. $A_{k}$ is constructed and each $A_{k}$ is used as an ordering transformation the $B_{j}$ 's to obtain a set of matrices $U[j, k]$. The rows of $B_{j}, U[j, k]$, and the $f$ rows of $M$ constitute the set of desired sequences. If the sequence lengths is $n$ then algorithm generate $n$ set of sequences of following properties:

* Number of time divisions $=n$
* Number of symbols $=n^{2}$
* Sequence minimum distance $=n-1$
* Number of frequency divisions $=n^{2}$
* Number of sequences $=n^{2}\left(n^{2}+n+1\right)$


## CHAPTER

## REPRESENTATION OF RMA SYSTEM

A system is a collection of interacting elements or
components that act together to achieve a common goal
systems can be studied by direct experimentation by building
prototype or by building mathematical/models. The purpose of
study through modelling is to aid the analysis understanding
design, operation, prediction or control of systems without
actually constructing and operating the real thing.
simulation is the process of imitating the behaviour of the
real system by constructing and experimenting with a model
which is only simplified representation of the system.

### 3.1 Representing Work

Modelling we mean is the determination of those quantitative features which describe the operation of a system to study the system we take simpler system which resemble with the actual system.

Developing of model involves two tasks (i) developing a representation of the system, and (ii) developing a representation of the work done by the system, these are interested. Some considerations are as follows:

### 3.1.1 Variability

Most of the problems resources; this contention causes work to be quenched for or blocked from execution, and system performance may suffer as a result.

### 3.1.2 Choosing a Distribution

Determining what distribution use to represent most different variable is one of the most difficult aspects of the simulation modelling.

The most important distribution in the analysis of queuing system is the exponential distribution Random arrivals or random service, we mean that the inter-arrival times or the service times are exponentially distributed. We take poison arrivals because of the relationship between piosson and exponentially distribution.

An important property of the Poisson process is that it is in employees; the probability of an arrival in interval 't' depends only on the duration of $t$, and not on the previous arrival occurrence. Another merit of Poisson process is * that the super position of Poisson process is itself a Piosson process.

### 3.1.3 Sampling from Distribution

A particular value of a model variable is determined by
generating a random sample from the distribution specified for that variable we use a uniform random number generator to generate these samples; the uniform random number generator is a numerical algorithm which produces a deterministic sequence of values distributed between $O$ and 1.

### 3.2 Simulation model of RMA Codes Scheme

In RMA scheme, the user's messages are coded and an RMA sequenced are obtained. The messages are transmitted randomly and depend on their availability. so this could result in message overlapping but as seen from the figure 2 , every overlapping does not conclude in collision. This is because of the controlled overlapping provided by the orthogonality is coded sequences by the RMA code generation algorithm. However, we have limitation of the code length, it is not very large and one overlapping symbol has been allowed designing code generation there is district probability that two or more overlapping messages have the same code word and same time to result in a clash.

The various possible cases are shown in figure 2 to clear the condition of the clash.

It is clear from the figure that some part or all message which have same code word and same time of overlapping cause a clash.

### 3.3 Message Arrival Process:

For the purpose of simulation, a treatment carried out as follows. Th message are generated using Poisson probability distribution with exponential inter-arrival time (IAT). The probability that no message arrive before a time $T$ is given by the probability density function [4]
$P_{r}[T>t]=\lambda \quad e^{-\lambda t}$
where $\lambda$ is a positive constant. The distribution function $F(t)$ is the integral of density function i.e.

$$
F(t)=\int_{0}^{t} \lambda e^{-\lambda t} d t=1-e^{-\lambda t}
$$

The average or expected value of $t$ is given by

$$
\begin{aligned}
E(t) & =\int_{0}^{\phi} t e^{-t} d t \\
& =1 / \lambda
\end{aligned}
$$

So we define $\lambda$ as the inverse of mean inter-arrival time (MIAT). Since the distribution function $F(t)$ has a value varying between ' 0 ' and ' 1 ', this property can be used to derive exponentially distributed inter-arrival times utilising the inverse transformation function, as in figure 3.


Fig3 Arrival distribution function

Let $r$ be the random number between $O$ and 1 using one to one correspondence between this random number and the distribution function, we get

```
    \(r=1-e^{-\lambda t}\)
or \(\quad-\lambda t=\ln (1-r)\)
    \(t=-\ln (1-r) / \lambda\)
    \(t=F^{-1}(r)\)
    Since (1-r) has similar as \(r\) its randomness. we replace
it by \(r\),
```

$$
t_{k}=-\frac{1}{\lambda} \ln r_{k}
$$

```
therefore, for a given \(r_{k}\), a corresponding \(t_{k}\) can be found if know the arrival rate \(\lambda\).
So the arrival process is modelled through a Poisson point process with exponential distribution for interarrival times. Random numbers between ' \(O\) ' and ' 1 ' are used to determined the interarrival distribution function.
```


### 3.4 Channel Observation Process

The channel observation process is involved very much here is necessary, but not a sufficient condition for message clash. It is therefore required to actually compare the contents of the overlapped portion of the message to determine a clash. A Monte-Carlo technique is used to generate random streams of data bits in each message. Then depending upon the binary digit ' $O$ ' or ' 1 ' a corresponding RMA code sequence is assigned to each message, to achieve this the programme for the code sequence generation is made separately and the code sequence for various values of the code sequence length $n$; are determines.

These are stored in data file (RMACODE) which is read by the simulation program while assigning these code sequences; the channel observation process compares the overlapping message bit by bit to check the clash.

(a)

(b)

Overlappeng wilt same ceedr werrels buit they
are hat rist simuitanpers - Nir clish
(c)


$$
\begin{aligned}
& \text { Overlapping with same cocte words and } \\
& \text { they fixist simultaneous - Clash } \\
& \text { (d) }
\end{aligned}
$$

$$
\text { Firg }<\text { CLASH CONDITICN FOR RIMA }
$$

```
    Due to the random arrived of the message, it is
possible that there could be multiple overlaps i.e. message
no.1 could have overlap with message nos. 2,3&4. Each of
these messages has different contents and are generally
orthogonal to each other. It is however, quite likely that
message no.1 may not clash with message no.2 but it may
clash with message no.3 or 4.
    The channel observation process thus has to keep a
track of correct number of distinct message collisions, and
not to count a collided message twice.
3.5 Traffic Model
    Mean Interarrival Time (MIAT) which determines the
value of is based upon the actual traffic statistics of
the application in mind. Let we consider the following
traffic model.
No. of nodes or user =N
No. of message/node =M
No. of bits/message = W
    Considering t hrs working day in which all the M
messages in each node has to be cleared transmission bit
rate required is given by
```

```
    Bit rate = = N < M x W 
    average number of message arriving at the satellite
channel per second is given by
    = N N MM
    if the traffic per node is higher or lower then this
average value of would according be higher (say 20) and
lower (say 1).
    The above figures represent a realistic network of a
typical thin traffic, large user application. However, due
to computational constraints and for easiness of simulation
while keeping the same values. The following model is
chosen
No. of users = 100 = N
No. of message/node/day = 3000=M
No. of bits/message = 100 = W
Transmission bit rate = 0.8328 kbps
    In the above figures, though transmission bit rate is
not required for simulation purpose, it is kept for the sake
of completeness and to indicate the typical value for the
application is mind
```


### 3.6 Throughput Computation

```
    Let us define the "message time" [4] as the amount of
time needed to transmit a fixed length message (i.e. message
lengths divided by the bit rate) on the traffic model
chosen, we have computed approximately }10\mathrm{ message per second
which for the chosen transmission bit rate would led to one
message per message time. However, if we increased or
decreased the traffic loading and kept the same transmission
bit rate. The number of message per message time would also
increase or decrease respectively.
The number of message offered per message time is defined as the offered traffic \(Z\). Throughput \(T P\) is computed at different offered traffic, which is varied by changing the value of mean inter arrival time.
```

CHAPTER 4

RESULTS OF THE PROGRAM


| $\mathrm{U}(0,2)$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 4 | 15 | 17 | 50 |
| 6 | 12 | 19 | 49 |
| 5 | 14 | 16 | 51 |
| 7 | 13 | 18 | 48 |
| U (0, 3) |  |  |  |
| 4 | 14 | 19 | 49 |
| 5 | 12 | 18 | 51 |
| 7 | 13 | 16 | 50 |
| 6 | 15 | 17 | 48 |
| $\mathrm{B1}=$ |  |  |  |
| 8 | 16 | 20 | 52 |
| 9 | 17 | 21 | 53 |
| 10 | 18 | 22 | 54 |
| 11 | 19 | 23 | 55 |
| $\mathrm{U}(1,1)$ |  |  |  |
| 8 | 17 | 22 | 55 |
| 11 | 16 | 21 | 54 |
| 10 | 19 | 20 | 53 |
| 9 | 18 | 23 | 52 |
| $\mathrm{U}(1,2)$ |  |  |  |
| 8 | 19 | 21 | 54 |
| 10 | 16 | 23 | 53 |
| 9 | 18 | 20 | 55 |
| 11 | 17 | 22 | 52 |
| $\mathrm{U}(1,3)$ |  |  |  |
| 8 | 18 | 23 | 53 |
| 9 | 16 | 22 | 55 |
| 11 | 17 | 20 | 54 |
| 10 | 19 | 21 | 52 |
| B2 = |  |  |  |
| 12 | 20 | 24 | 56 |
| 13 | 21 | 25 | 57 |
| 14 | 22 | 26 | 58 |
| 15 | 23 | 27 | 59 |
| $\mathrm{U}(2,1)$ |  |  |  |
| 12 | 21 | 26 | 59 |
| 15 | 20 | 25 | 58 |
| 14 | 23 | 24 | 57 |
| 13 | 22 | 27 | 56 |
| $\mathrm{U}(2,2)$ |  |  |  |
| 12 | 23 | 25 | 58 |
| 14 | 20 | 27 | 57 |
| 13 | 22 | 24 | 59 |
| 15 | 21 | 26 | 56 |

$$
T H-5594
$$

| U ( 2,3$)$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 12 | 22 | 27 | 57 |
| 13 | 20 | 26 | 59 |
| 15 | 21 | 24 | 58 |
| 14 | 23 | 25 | 56 |
| B3 $=$ |  |  |  |
| 16 | 24 | 28 | 0 |
| 17 | 25 | 29 | 1 |
| 18 | 26 | 30 | 2 |
| 19 | 27 | 31 | 3 |
| U ( 3,1 ) |  |  |  |
| 16 | 25 | 30 | 3 |
| 19 | 24 | 29 | 2 |
| 18 | 27 | 28 | 1 |
| 17 | 26 | 31 | 0 |
| $\mathrm{U}(3,2)$ |  |  |  |
| 16 | 27 | 29. | 2 |
| 18 | 24 | 31 | 1 |
| 17 | 26 | 28 | 3 |
| 19 | 25 | 30 | 0 |
| U ( 3,3$)$ |  |  |  |
| 16 | 26 | 31 | 1 |
| 17 | 24 | 30 | 3 |
| 19 | 25 | 28 | 2 |
| 18 | 27 | 29 | 0 |
| $\mathrm{B4}=$ |  |  |  |
| 20 | 28 | 32 | 4 |
| 21 | 29 | 33 | 5 |
| 22 | 30 | 34 | 6 |
| 23 | 31 | 35 | 7 |
| U (4, 1) |  |  |  |
| 20 | 29 | 34 | 7 |
| 23 | 28 | 33 | 6 |
| 22 | 31 | 32 | 5 |
| 21 | 30 | 35 | 4 |
| $\mathrm{U}(4,2)$ |  |  |  |
| 20 | 31 | 33 | 6 |
| 22 | 28 | 35 | 5 |
| 21 | 30 | 32 | 7 |
| 23 | 29 | 34 | 4 |
| $\mathrm{U}(4,3)$ |  |  |  |
| 20 | 30 | 35 | 5 |
| 21 | 28 | 34 | 7 |
| 23 | 29 | 32 | 6 |
| 22 | 31 | 33 | 4 |


| B5 = |  |  |  |
| :---: | :---: | :---: | :---: |
| 24 | 32 | 36 | 8 |
| 25 | 33 | 37 | 9 |
| 26 | 34 | 38 | 10 |
| 27 | 35 | 39 | 11 |
| $U(5,1)$ |  |  |  |
| 24 | 33 | 38 | 11 |
| 27 | 32 | 37 | 10 |
| 26 | 35 | 36 | 9 |
| 25 | 34 | 39 | 8 |
| U (5, 2 ) |  |  |  |
| 24 | 35 | 37 | 10 |
| 26 | 32 | 39 | 9 |
| 25 | 34 | 36 | 11 |
| 27 | 33 | 38 | 8 |
| $\mathrm{U}(5,3)$ |  |  |  |
| 24 | 34 | 39 | 9 |
| 25 | 32 | 38 | 11 |
| 27 | 33 | 36 | 10 |
| 26 | 35 | 37 | 8 |
| $\mathrm{B6}=$ |  |  |  |
| 28 | 36 | 40 | 12 |
| 29 | 37 | 41 | 13 |
| 30 | 38 | 42 | 14 |
| 31 | 39 | 43 | 15 |
| U (6, 1) |  |  |  |
| 28 | 37 | 42 | 15 |
| 31 | 36 | 41 | 14 |
| 30 | 39 | 40 | 13 |
| 29 | 38 | 43 | 12 |
| U (6, 2 ) |  |  |  |
| 28 | 39 | 41 | 14 |
| 30 | 36 | 43 | 13 |
| 29 | 38 | 40 | 15 |
| 31 | 37 | 42 | 12 |
| U (6, 3) |  |  |  |
| 28 | 38 | 43 | 13 |
| 29 | 36 | 42 | 15 |
| 31 | 37 | 40 | 14 |
| 30 | 39 | 41 | 12 |
| B7 = |  |  |  |
| 32 | 40 | 44 | 16 |
| 33 | 41 | 45 | 17 |
| 34 | 42 | 46 | 18 |
| 35 | 43 | 47 | 19 |


| $\mathrm{U}(7,1)$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 32 | 41 | 46 | 19 |
| 35 | 40 | 45 | 18 |
| 34 | 43 | 44 | 17 |
| 33 | 42 | 47 | 16 |
| $\mathrm{U}(7,2)$ |  |  |  |
| 32 | 43 | 45 | 18 |
| 34 | 40 | 47 | 17 |
| 33 | 42 | 44 | 19 |
| 35 | 41 | 46 | 16 |
| $\mathrm{U}(7,3)$ |  |  |  |
| 32 | 42 | 47 | 17 |
| 33 | 40 | 46 | 19 |
| 35 | 41 | 44 | 18 |
| 34 | 43 | 45 | 16 |
| B8 = |  |  |  |
| 36 | 44 | 48 | 20 |
| 37 | 45 | 49 | 21 |
| 38 | 46 | 50 | 22 |
| 39 | 47 | 51 | 23 |
| $\mathrm{U}(8,1)$ |  |  |  |
| 36 | 45 | 50 | 23 |
| 39 | 44 | 49 | 22 |
| 38 | 47 | 48 | 21 |
| 37 | 46 | 51 | 20 |
| $\mathrm{U}(8,2)$ |  |  |  |
| 36 | 47 | 49 | 22 |
| 38 | 44 | 51 | 21 |
| 37 | 46 | 48 | 23 |
| 39 | 45 | 50 | 20 |
| $\mathrm{U}(8,3)$ |  |  |  |
| 36 | 46 | 51 | 21 |
| 37 | 44 | 50 | 23 |
| 39 | 45 | 48 | 22 |
| 38 | 47 | 49 | 20 |
| B9 = |  |  |  |
| 40 | 48 | 52 | 24 |
| 41 | 49 | 53 | 25 |
| 42 | 50 | 54 | 26 |
| 43 | 51 | 55 | 27 |
| $\mathrm{U}(9,1)$ |  |  |  |
| 40 | 49 | 54 | 27 |
| 43 | 48 | 53 | 26 |
| 42 | 51 | 52 | 25 |
| 41 | 50 | 55 | 24 |


| $\mathrm{U}(9,2)$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 40 | 51 | 53 | 26 |
| 42 | 48 | 55 | 25 |
| 41 | 50 | 52 | 27 |
| 43 | 49 | 54 | 24 |
| $U(9,3)$ |  |  |  |
| 40 | 50 | 55 | 25 |
| 41 | 48 | 54 | 27 |
| 43 | 49 | 52 | 26 |
| 42 | 51 | 53 | 24 |
| B10 |  |  |  |
| 44 | 52 | 56 | 28 |
| 45 | 53 | 57 | 29 |
| 46 | 54 | 58 | 30 |
| 47 | 55 | 59 | 31 |
| $\mathrm{U}(10,1)$ |  |  |  |
| 44 | 53 | 58 | 31 |
| 47 | 52 | 57 | 30 |
| 46 | 55 | 56 | 29 |
| 45 | 54 | 59 | 28 |
| $\mathrm{U}(10,2)$ |  |  |  |
| 44 | 55 | 57 | 30 |
| 46 | 52 | 59 | 29 |
| 45 | 54 | 56 | 31 |
| 47 | 53 | 58 | 28 |
| $\mathrm{U}(10,3)$ |  |  |  |
| 44 | 54 | 59 | 29 |
| 45 | 52 | 58 | 31 |
| 47 | 53 | 56 | 30 |
| 46 | 55 | 57 | 28 |
| $\mathrm{B11}=$ |  |  |  |
| 48 | 56 | 0 | 32 |
| 49 | 57 | 1 | 33 |
| 50 | 58 | 2 | 34 |
| 51 | 59 | 3 | 35 |
| $\mathrm{U}(11,1)$ |  |  |  |
| 48 | 57 | 2 | 35 |
| 51 | 56 | 1 | 34 |
| 50 | 59 | 0 | 33 |
| 49 | 58 | 3 | 32 |
| $\mathrm{U}(11,2)$ |  |  |  |
| 48 | 59 | 1 | 34 |
| 50 | 56 | 3 | 33 |
| 49 | 58 | 0 | 35 |
| 51 | 57 | 2 | 32 |


| U (11, 3) |  |  |  |
| :---: | :---: | :---: | :---: |
| 48 | 58 | 3 | 33 |
| 49 | 56 | 2 | 35 |
| 51 | 57 | 0 | 34 |
| 50 | 59 | 1 | 32 |
| B12 |  |  |  |
| 52 | 0 | 4 | 36 |
| 53 | 1 | 5 | 37 |
| 54 | 2 | 6 | 38 |
| 55 | 3 | 7 | 39 |
| $\mathrm{U}(12,1)$ |  |  |  |
| 52 | 1 | 6 | 39 |
| 55 | 0 | 5 | 38 |
| 54 | 3 | 4 | 37 |
| 53 | 2 | 7 | 36 |
| $\mathrm{U}(12,2)$ |  |  |  |
| 52 | 3 | 5 | 38 |
| 54 | 0 | 7 | 37 |
| 53 | 2 | 4 | 39 |
| 55 | 1 | 6 | 36 |
| $\mathrm{U}(12,3)$ |  |  |  |
| 52 | 2 | 7 | 37 |
| 53 | 0 | 6 | 39 |
| 55 | 1 | 4 | 38 |
| 54 | 3 | 5 | 36 |
| B13 |  |  |  |
| 56 | 4 | 8 | 40 |
| 57 | 5 | 9 | 41 |
| 58 | 6 | 10 | 42 |
| 59 | 7 | 11 | 43 |
| $\mathrm{U}(13,1)$ |  |  |  |
| 56 | 5 | 10 | 43 |
| 59 | 4 | 9 | 42 |
| 58 | 7 | 8 | 41 |
| 57 | 6 | 11 | 40 |
| U (13, 2 ) |  |  |  |
| 56 | 7 | 9 | 42 |
| 58 | 4 | 11 | 41 |
| 57 | 6 | 8 | 43 |
| 59 | 5 | 10 | 40 |
| U (13, 3) |  |  |  |
| 56 | 6 | 11 | 41 |
| 57 | 4 | 10 | 43 |
| 59 | 5 | 8 | 42 |
| 58 | 7 | 9 | 40 |


| B14 $=$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | 8 | 12 | 44 |
| 1 | 9 | 13 | 45 |
| 2 | 10 | 14 | 46 |
| 3 | 11 | 15 | 47 |
| U ( 14,1 ) |  |  |  |
| 0 | 9 | 14 | 47 |
| 3 | 8 | 13 | 46 |
| 2 | 11 | 12 | 45 |
| 1 | 10 | 15 | 44 |
| U ( 14,2 ) |  |  |  |
| 0 | 11 | 13 | 46 |
| 2 | 8 | 15 | 45 |
| 1 | 10 | 12 | 47 |
| 3 | 9 | 14 | 44 |
| U ( 14,3 ) |  |  |  |
| 0 | 10 | 15 | 45 |
| 1 | 8 | 14 | 47 |
| 3 | 9 | 12 | 46 |
| 2 | 11 | 13 | 44 |
| B15 $=$ |  |  |  |
| 0 | 20 | 40 | 60 |
| 1 | 21 | 41 | 61 |
| 2 | 22 | 42 | 62 |
| 3 | 23 | 43 | 63 |
| $\mathrm{U}(15,1)$ |  |  |  |
| 0 | 21 | 42 | 63 |
| 3 | 20 | 41 | 62 |
| 2 | 23 | 40 | 61 |
| 1 | 22 | 43 | 60 |
| $\mathrm{U}(15,2)$ |  |  |  |
| 0 | 23 | 41 | 62 |
| 2 | 20 | 43 | 61 |
| 1 | 22 | 40 | 63 |
| 3 | 21 | 42 | 60 |
| $\mathrm{U}(15,3)$ |  |  |  |
| 0 | 22 | 43 | 61 |
| 1 | 20 | 42 | 63 |
| 3 | 21 | 40 | 62 |
| 2 | 23 | 41 | 60 |
| $\mathrm{B} 16=$ |  |  |  |
| 4 | 24 | 44 | 60 |
| 5 | 25 | 45 | 61 |
| 6 | 26 | 46 | 62 |
| 7 | 27 | 47 | 63 |


| U ( 16,1 ) |  |  |  |
| :---: | :---: | :---: | :---: |
| 4 | 25 | 46 | 63 |
| 7 | 24 | 45 | 62 |
| 6 | 27 | 44 | 61 |
| 5 | 26 | 47 | 60 |
| $\mathrm{U}(16,2)$ |  |  |  |
| 4 | 27 | 45 | 62 |
| 6 | 24 | 47 | 61 |
| 5 | 26 | 44 | 63 |
| 7 | 25 | 46 | 60 |
| $\mathrm{U}(16,3)$ |  |  |  |
| 4 | 26 | 47 | 61 |
| 5 | 24 | 46 | 63 |
| 7 | 25 | 44 | 62 |
| 6 | 27 | 45 | 60 |
| $\mathrm{B17}=$ |  |  |  |
| 8 | 28 | 48 | 60 |
| 9 | 29 | 49 | 61 |
| 10 | 30 | 50 | 62 |
|  | 31 | 51 | 63 |
| $\mathrm{U}(17,1)$ |  |  |  |
| 8 | 29 | 50 | 63 |
| 11 | 28 | 49 | 62 |
| 10 | 31 | 48 | 61 |
| 9 | 30 | 51 | 60 |
| $\mathrm{U}(17,2)$ |  |  |  |
| 8 | 31 | 49 | 62 |
| 10 | 28 | 51 | 61 |
| 9 | 30 | 48 | 63 |
| 11 | 29 | 50 | 60 |
| $\mathrm{U}(17,3)$ |  |  |  |
| 8 | 30 | 51 | 61 |
| 9 | 28 | 50 | 63 |
| 11 | 29 | 48 | 62 |
| 10 | 31 | 49 | 60 |
| $\mathrm{B18}=$ |  |  |  |
| 12 | 32 | 52 | 60 |
| 13 | 33 | 53 | 61 |
| 14 | 34 | 54 | 62 |
| 15 | 35 | 55 | 63 |
| $\mathrm{U}(18,1)$ |  |  |  |
| 12 | 33 | 54 | 63 |
| 15 | 32 | 53 | 62 |
| 14 | 35 | 52 | 61 |
| 13 | 34 | 55 | 60 |


| $N \omega \bullet \bigcirc \underset{\omega}{\omega}$ | $\omega \vdash N O$ N | －NWOP | $\stackrel{\leftrightarrow}{\infty} \stackrel{\rightharpoonup}{\circ} \text { の }$ | $\stackrel{\rightharpoonup}{\bullet} \stackrel{\omega}{\infty} \text { の }$ |  |  |  | $\stackrel{\leftrightarrow}{\hookrightarrow} \stackrel{\leftrightarrow}{\omega} \stackrel{( }{\sim}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\omega$－${ }^{\text {O }}$ | －NOW | N ${ }^{\text {O－}}$ |  | $\stackrel{\rightharpoonup}{6}$ | $\bigcirc$ |  | $\infty$ | $\infty$ |
|  |  |  | $\begin{array}{llll}\omega & \omega & \omega \\ \omega & \sim\end{array}$ | $\cdots$ | $\begin{array}{llll}\omega & \omega & \omega \\ \infty & 0 & \omega & \omega \\ \end{array}$ |  | ${ }_{\sim}^{\omega}{ }_{\omega}^{\omega} \stackrel{\omega}{\sim} \stackrel{\omega}{\Delta} \dot{\omega}$ |  |
| －ONW | Now | $\omega \bigcirc \mapsto N$ |  |  |  |  |  |  |
|  |  |  | GUGU | GuGu | GGGu | ungu | Gugu | GUGG |
| ○Nルー | OんトN | $\bigcirc \bullet N \omega$ | ソのが | $\infty$ の 0 | ¢のコロ | $6 \infty$ の | $\omega N \sim G$ | －NGW |
|  |  |  | Og an | oqa | $\begin{gathered} \sigma \\ 0 \\ 0 \\ \end{gathered}$ | $\underset{\omega}{0} \underset{\sim}{\circ} \dot{0}$ | aga | aga |

## 4.2

Sequence Length $=3$
Packet Transmission time $=0.1 \mathrm{sec}$
Channel speed $=1000 \mathrm{Bits} / \mathrm{Sec}$.
Number of Packet $=60$

| Nclash | Lamda | Z | TP |
| :---: | :---: | :---: | :---: |
| 7 |  |  |  |
| 5 | 1 | 0.1 | 0.08 |
| 5 | 2 | 0.2 | 0.11 |
| 24 | 3 | 0.3 | 0.13 |
| 29 | 5 | 0.4 | 0.17 |
| 27 | 6 | 0.5 | 0.20 |
| 38 | 7 | 0.7 | 0.22 |
| 41 | 8 | 0.8 | 0.24 |
| 43 | 9 | 0.9 | 0.26 |
| 38 | 10 | 1.0 | 0.27 |
| 39 | 11 | 1.1 | 0.27 |
| 42 | 12 | 1.2 | 0.25 |
| 43 | 13 | 1.3 | 0.21 |
| 46 | 14 | 1.4 | 0.20 |
| 48 | 15 | 1.5 | 0.15 |
| 48 | 16 | 1.6 | 0.14 |
| 49 | 18 | 1.7 | 0.14 |
| 53 | 19 | 1.8 | 0.14 |
| 53 | 20 | 2.0 | 0.13 |
| 54 |  |  | 0.12 |

Sequence Length $=4$
Packet Transmission time $=0.1 \mathrm{sec}$
Channel Speed $=1000$ bits $/ \mathrm{Sec}$
Number of Packets $=60$

| Nclash | Lamda | Z | TP |
| :---: | :---: | :---: | :---: |
| 7 |  |  |  |
| 7 | 1 | 0.1 | 0.09 |
| 9 | 2 | 0.2 | 0.17 |
| 10 | 3 | 0.3 | 0.24 |
| 13 | 4 | 0.4 | 0.33 |
| 18 | 5 | 0.5 | 0.39 |
| 21 | 6 | 0.6 | 0.46 |
| 20 | 7 | 0.7 | 0.49 |
| 23 | 8 | 0.8 | 0.53 |
| 24 | 9 | 0.9 | 0.55 |
| 21 | 10 | 1.0 | 0.60 |
| 25 | 11 | 1.1 | 0.64 |
| 27 | 13 | 1.2 | 0.65 |
| 31 | 14 | 1.3 | 0.68 |
| 38 | 15 | 1.4 | 0.69 |
| 38 | 16 | 1.5 | 0.71 |
| 38 | 17 | 1.6 | 0.73 |
| 38 | 18 | 1.7 | 0.76 |
| 39 | 19 | 1.8 | 0.82 |
| 39 | 20 | 1.9 | 0.83 |
| 39 |  | 2.0 | 0.84 |

Sequence Length $=4$
Packet transmission time $=0.1 \mathrm{sec}$
Channel speed $=1000 \mathrm{bits} / \mathrm{sec}$
Number of Packets $=120$

| Nclash | Lamda | Z | TP |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 8 | 1 | 0.1 | 0.09 |
| 23 | 2 | 0.2 | 0.16 |
| 39 | 3 | 0.3 | 0.23 |
| 52 | 4 | 0.4 | 0.29 |
| 42 | 5 | 0.5 | 0.37 |
| 47 | 6 | 0.6 | 0.42 |
| 50 | 7 | 0.7 | 0.46 |
| 63 | 8 | 0.8 | 0.47 |
| 61 | 9 | 0.9 | 0.51 |
| 61 | 10 | 1.0 | 0.53 |
| 64 | 12 | 1.1 | 0.55 |
| 66 | 13 | 1.2 | 0.56 |
| 68 | 14 | 1.3 | 0.58 |
| 68 | 15 | 1.4 | 0.59 |
| 72 | 16 | 1.5 | 0.59 |
| 72 | 17 | 1.6 | 0.60 |
| 73 | 18 | 1.7 | 0.63 |
| 74 | 20 | 1.8 | 0.64 |
| 76 |  | 1.9 | 0.66 |
| 76 |  | 2.0 | 0.68 |

## performance of RMA



## Performance of RMA



## Performance of RMA



FIG $4 . c$
Fer $n=4$, Packids 120

## Performance of RMA



FIG 4.d

## Performance of RMA



FIG $4 . e$

## CHAPTER 5

## CONCLUSION

Using the RMA codes sequences, the simulation is carried out and performance evaluation of the system is done by calculating the channel throughput. The simulation programs in written in Pascal.

### 5.1 RMA code generation

We generated RMA code for sequence length 3 and 4 . The RMA code sequences which are attached to this work tally with the given one for sequence length 4 [5]. The results for $n=3$ also tally.

### 5.2 Simulation

This is the main task of this work. We calculated channel throughput for varying offered load. We get the results (chapter 4). We see that results are better than Pure ALOHA[4]. In this work channel throughput for $n=3,4$ at varying load is obtained and graphs are also drawn between throughput and offered load (Fig.4.a). We have taken the above for the different packet numbers i.e. packet number 60 and 120. It is observed from these graphs that the varying load with a graceful degradation for high value of traffic rate. We see that as the number of packet increases the
number of clashes increases. As the number of packet increase the throughput decreases (Fig.4.e). As the offered load values increases throughput increases. We see that curve does not change the slope from positive to negative (Fig.4.b and 4.c). As the sequence length increases number of clashes increases and throughput decreases (Fig.4.a, Fig. $4 . b$.

## Conclusion

The RMA CODE algorithm which is given by W.W.Wu has great potential in improvement the satellite communication application where it can be entertained by large number of users. For sequence length four, we get 336 coded seqeunces (Chapter 4).

Hence, we tried to obtain the channel throughput as a performance measure at varying traffic load and different packet numbers and also at different sequence length.

We can implement this to VLSI and transistor level simulation can be done.

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## APPENDIX

FLOW CHART FOR RMA SIMULATION PROGRAM







## PROCEDURE RANDOM


\{This program generate RMA coded sequences, which
are to be used further for the simulation purpose. \}
Program RMACODE(input,output,fout);
const $\mathrm{n}=4$; (* sequence lenth *)
$\mathrm{d} 0=1 ; \mathrm{dl}=3 ; \mathrm{d} 2=4 ; \mathrm{d} 3=12 ;\left(\right.$ these are euclidean distances $\left.{ }^{*}\right)$

```
var i,j,p,k,s :integer;
    q,r,ml,t,v :integer;
    w0 :array [0.. (n*n+n-1),0..n-1] of integer;
    m :array[0..n*n-1,0..n-1] of integer;
    b :array[0..n*n+n-1,0..n-1] of integer;
    a,al,b1,u :array[0..n-1,0..n] of integer;
    fout :text;
```

procedure order(s,p,q,r:integer);
begin
$\mathrm{u}[0,0]:=\mathrm{b}[\mathrm{s}, 0] ; \mathrm{u}[1,0]:=\mathrm{b}[\mathrm{p}, 0] ;$
$\mathrm{u}[2,0]:=\mathrm{b}[\mathrm{q}, 0] ; \mathrm{u}[3,0]:=\mathrm{b}[\mathrm{r}, 0]$;
$\mathrm{u}[0,1]:=\mathrm{b}[\mathrm{r}, 1] ; \mathrm{u}[1,1]:=\mathrm{b}[\mathrm{s}, 1] ;$
$\mathrm{u}[2,1]:=\mathrm{b}[\mathrm{p}, 1] ; \mathrm{u}[3,1]:=\mathrm{b}[\mathrm{q}, 1] ;$
$\mathrm{u}[0,2]:=\mathrm{b}[\mathrm{q}, 2] ; \mathrm{u}[1,2]:=\mathrm{b}[\mathrm{r}, 2]$;
$\mathrm{u}[2,2]:=\mathrm{b}[\mathrm{s}, 2] ; \mathrm{u}[3,2]:=\mathrm{b}[\mathrm{p}, 2] ;$
$\mathrm{u}[0,3]:=\mathrm{b}[\mathrm{p}, 3] ; \mathrm{u}[1,3]:=\mathrm{b}[\mathrm{q}, 3] ;$
$\mathrm{u}[2,3]:=\mathrm{b}[\mathrm{r}, 3] ; \mathrm{u}[3,3]:=\mathrm{b}[\mathrm{s}, 3] ;$
end;
begin
assign(fout,'rmacode');
rewrite(fout);
$w 0[0,0]:=\mathrm{d} 0 ; \quad \mathrm{w} 0[0,1]:=\mathrm{d} 1$;
$\mathrm{w} 0[0,2]:=\mathrm{d} 2 ; \quad \mathrm{w} 0[0,3]:=\mathrm{d} 3$;
writeln(fout,'RMACODE SEQUENCES ARE AS FOLLOWS');
writeln(fout, 'w0');

(*-------------To generate W0 matrix------------------*)
for $\mathrm{i}:=1$ to $\left(\mathrm{n}^{*} \mathrm{n}-1\right)$ do
begin
writeln(fout);
for $\mathrm{j}:=0$ to ( $\mathrm{n}-1$ ) do
begin

```
        w0[i,j]:=(w0[0,j]+i) mod (n*n-1);
        write(fout,w0[i-1,j],' ');
        end;
    end;
    writeln(fout); writeln(fout);
    writeln(fout); writeln(fout);
(*------------- To generate the W1 matrix--------------**)
    writeln(fout,'wl');
    writeln(fout,'--------------------------------');
    for i :=(n*n-1) to (n*n+n-1) do
    w0[i,n-1]:=(n*n-1);
    p:=0;
    for i:=(n*n-1) to (n*n+n-1) do
    begin
        for j:=0 to n-2 do
        begin
            wO[i,j]:= (j*(n+1)+p) mod(n*n-1);
            write(fout,w0[i,j],' ');
        end;
            writeln (fout,w0[i,n-1]);
            p:=p+1;
    end;
(*-----------------To construct M matrix-----------------*)
    writeln(fout);
    writeln(fout,'M');
    writeln(fout,'---------------------------------})
    for i:=0 to n-1 do
    m[0,i]:= i;
    for i:=1 to (n*n-1) do
    begin
        for j:=0 to n-1 do
            begin
                m[i,j]:=m[i-1,j]+n;
                write(fout,m[i-1,j],' ');
        end;
            writeln(fout);
    end;
```

(*-----To get sequences from the combination of above----------**)

```
for t:=0 to (n*n+n-1) do
    begin
    writeln(fout,'B',t,' =');
    for v:=0 to n-1 do
    begin
        for j:=0 to (n-1) do
        begin
            b[v,j]:=n*w0[t,j]+v;
            write(fout,b[v,j],' ');
        end;
            writeln(fout);
    end;
    for ml:=1 to n-1 do
    begin
        case ml of
            1:begin
                s:=0; p:=3;
                    q:=2; r:=1;
                        order(s,p,q,r);
                end;
            2 : begin
                    s:=0; p:=2;
                    q:=1; r:=3;
                    order(s,p,q,r);
                end;
            3:begin
                                    s:=0; p:=1;
                                    q:=3; r:=2;
                order(s,p,q,r);
                end;
            end; (*end of case*)
    writeln(fout,'U(',t,',',ml,')');
    for i:=0 to n-1 do
    begin
        for j:=0 to n-1 do
        begin
            write(fout,u[i,j],' ');
        end;
            writeln(fout);
    end;
end;
```

end;
writeln(fout);
(*--------To construct the permutation matrices--------------...--*)

$$
\begin{aligned}
& \mathrm{k}:=1 ; \\
& \text { if } \mathrm{k}=1 \text { then } \\
& \text { begin } \\
& \text { writeln(fout,' } \left.\mathrm{A}^{\prime}, \mathrm{k}\right) ; \\
& \text { for } \mathrm{i}:=0 \text { to } \mathrm{n}-1 \text { do } \\
& \text { begin } \\
& \mathrm{a}[0, \mathrm{i}]:=\mathrm{i} ; \\
& \mathrm{a} \text {; }[0, \mathrm{i}]:=\mathrm{i} \text {; } \\
& \text { end; } \\
& \\
& \text { for } \mathrm{i}:=1 \text { to } \mathrm{n}-1 \text { do } \\
& \text { begin } \\
& \text { for } \mathrm{j}:=0 \text { to } \mathrm{n}-1 \text { do } \\
& \mathrm{a}[\mathrm{i}, \mathrm{j}+1]:=\mathrm{a}[\mathrm{i}-1, \mathrm{j}] ; \\
& \mathrm{a}[\mathrm{i}, 0]:=\mathrm{a}[\mathrm{i}-1, \mathrm{n}-1] ; \\
& \text { end; } \\
& \text { end; }
\end{aligned}
$$

for $\mathrm{i}:=0$ to $\mathrm{n}-1$ do begin for $\mathrm{j}:=0$ to $\mathrm{n}-1$ do write (fout, a[i,j],' '); writeln(fout);
end;
writeln(fout);
for $k:=2$ to $n-1$ do begin writeln(fout,' ${ }^{\prime}$ ',k); begin $\mathrm{i}:=0$;
for $\mathrm{j}:=1$ to $\mathrm{n}-2$ do
$\mathrm{a}[\mathrm{i}, \mathrm{j}+1]:=\mathrm{a} 1[0, \mathrm{j}]$;
$\mathrm{a}[\mathrm{i}, 0]:=0$;
$\mathrm{a}[\mathrm{i}, 1]:=\mathrm{n}-\mathrm{k}+1$;
for $\mathrm{j}:=0$ to $\mathrm{n}-1$ do

```
            al[0,j]:=a[0,j];
end;
    for i:=1 to n-1 do
    begin
        for j:=0 to n-1 do
            a[i,j+1]:= a[i-1,j];
        a[i,0] := a[i-1,n-1];
    end;
            for i:=0 to n-1 do
            begin
            for j:=0 to n-1 do
            write (fout,a[i,j],' ');
            writeln(fout);
            end;
end;
```



```
close(fout);
end.
```

